



# فرمول های مشتق گیری

در تمام فرمول های زیر  $w$ ,  $r$  و  $u$  بر حسب  $x$  فرض شده اند.

| تابع                    | مشتق                                  | مثال  |
|-------------------------|---------------------------------------|---|
| $y = a$                 | $y' = 0$                              | $y = 3 \Rightarrow y' = 0$  |
| $y = ax$                | $y' = a$                              | $y = 7x \Rightarrow y' = 7$   |
| $y = ax^n$              | $y' = a.nx^{n-1}$                     | $y = 2x^3 \Rightarrow y' = 2 \times 3 \times x^2$   |
| $y = u \pm v \pm \dots$ | $y' = u' \pm v' \pm \dots$            | $y = 3x^2 - 5x + 7 \Rightarrow y' = 6x - 5$   |
| $y = u.v$               | $y' = u'.v + v'.u$                    | $y = (3x^4)(\sin x) \Rightarrow y' = (12x^3)\sin x + (\cos x).3x^4$                                 |
| $y = au$                | $y' = au'$                            | $y = 5\cos \Rightarrow y' = -5\sin x$   |
| $y = \frac{u}{v}$       | $y' = \frac{u'.v - v'.u}{v^2}$        | $y = \frac{3x^2}{\tan x} \Rightarrow y' = \frac{6x(\tan x) - (1 + \tan^2 x)3x^2}{\tan^2 x}$         |
| $y = \frac{u}{a}$       | $y' = \frac{u'}{a}$                   | $y = \frac{\cot x}{5} \Rightarrow y' = \frac{-(1 + \cot^2 x)}{5}$                                   |
| $y = \frac{a}{u}$       | $y' = \frac{-au'}{u^2}$               | $y = \frac{3}{x^5} \Rightarrow y' = \frac{-3(5x^4)}{x^{10}} = \frac{-15}{x^6}$                      |
| $y = \frac{au+b}{cu+d}$ | $y' = \frac{ad-bc}{(cu+d)^2}u'$       | $y = \frac{3x+5}{2x-7} \Rightarrow y' = \frac{21-10}{(2x-7)^2} = \frac{-31}{(2x-7)^2}$              |
| $y = au^m$              | $y' = m.a.u'.u^{m-1}$                 | $y = 5(\sin^2 x) \Rightarrow y' = 4 \times 5 \times \cos x \times \sin^3 x$                         |
| $y = \sqrt{u}$          | $y' = \frac{u'}{2\sqrt{u}}$           | $y = \sqrt{x} \Rightarrow y' = \frac{1}{2\sqrt{x}}$   |
| $y = \sqrt[m]{n^m}$     | $y' = \frac{nu'}{m\sqrt[m]{u^{m-n}}}$ | $y = \sqrt[5]{x^3} \Rightarrow y' = \frac{3}{5\sqrt[5]{x^2}}$                                       |
| $y =  u $               | $y' = \frac{u'.u}{ u }$               | $y =  x^2 + x  \Rightarrow y' = \frac{(2x+1)(x^2+x)}{ x^2+x }$                                      |
| $y = a \sin u$          | $y' = au' \cos u$                     | $y = -3\sin(2x^3 + 5) \Rightarrow y' = (-3)(6x^2)\cos(2x^3 + 5) = -18x^2 \cos(2x^3 + 5)$            |
| $y = a \cos u$          | $y' = -au' \sin u$                    | $y = 3\cos(\sqrt{x}) \Rightarrow y' = -(3)(\frac{1}{2\sqrt{x}}).\sin\sqrt{x}$                       |
| $y = a \tan u$          | $y' = au'(1 + \tan^2 u)$              | $y = 3\tan(\cos) \Rightarrow y' = 3(-\sin x)(1 + \tan^2(\cos x))$                                   |
| $y = a \cot u$          | $y' = -au'(1 + \cot^2 u)$             | $y = 5\cot x \Rightarrow y' = -5(1 + \cot^2 x)$   |
| $y = a \sin^m u$        | $y' = mau' \cos u \sin^{m-1} u$       | $y = 2\sin^3(x^5) \Rightarrow y' = (2 \times 3)(5x^4)(\cos(x^5))\sin^2(x^5)$                        |
| $y = a \cos^m u$        | $y' = -mau' \sin u \cos^{m-1} u$      | $y = 5\cos^4(\sqrt{x}) \Rightarrow y' = -(4)(5)(\frac{1}{2\sqrt{x}})(\sin\sqrt{x})(\cos^3\sqrt{x})$ |



|                        |   |  |
|------------------------|---|--|
| $y = a \tan^m u$       | $y' = mau'(1 + \tan^2 u) \tan^{m-1} u$                            | $y = 7 \tan^5 x \Rightarrow y' = 7 \times 5(1 + \tan^2 x) \tan^4 x$                  |
| $y = a \cot^m u$       | $y' = -mau'(1 + \cot^2 u) \cot^{m-1} u$                           | $y = 2 \cot^3 x \Rightarrow y' = -(3)(2)(1 + \cot^2 x) \cot^2 u$                     |
| $y = a \sec u$         | $y' = au' \cdot \sin u \cdot \sec^2 u$                            | $y = \sec x \Rightarrow y' = \sin \cdot \sec^2 u$                                    |
| $y = a \csc u$         | $y' = -au' \cos u \csc^2 u$                                       | $y = \csc(5x) \Rightarrow y' = -5 \cos(5x) \csc^2(5x)$                               |
| $y = \text{Arcsin}$    | $y' = \frac{u'}{\sqrt{1-u^2}}$                                    | $y = \text{Arcsin}(3x) \Rightarrow y' = \frac{3}{\sqrt{1-9x^2}}$                     |
| $y = \text{Arccos } u$ | $y' = \frac{-u'}{\sqrt{1-u^2}}$                                   | $y = \text{Arccos}(3x^2 - 5x) \Rightarrow y' = \frac{-(6x-5)}{\sqrt{1-(3x^2-5x)^2}}$ |
| $y = \text{Arctan } u$ | $y' = \frac{u'}{1+u^2}$   | $y = \text{Arctan } x \Rightarrow y' = \frac{1}{1+x^2}$                              |
| $y = \text{Arccot } u$ | $y' = \frac{-u'}{1+u^2}$  | $y = \text{Arccot}(\sin x) \Rightarrow y' = \frac{-\cos x}{1+\sin^2 x}$              |
| $y = a^u$              | $y' = u'a^u \ln a$  |  |
| $y = \sqrt{x}$         | $y' = \frac{1}{2\sqrt{x}}$  | $y = \sqrt{2} \Rightarrow y' = \frac{1}{2\sqrt{2}}$                                  |
| $y = \ln u$            | $y' = \frac{u'}{u}$   | $\ln e = 1 \checkmark$   |
| $y = \sin x$           | $y' = \cos x$   |  |
| $y = \cos x$           | $y' = -\sin x$  |  |
| $y = \tan x$           | $y' = 1 + \tan^2 x$   |  |
| $y = \cot x$           | $y' = -(1 + \cot^2 x)$  |  |
| $y = [u]$              | $y' = \begin{cases} 0 & u \notin z \\ \phi & u \in z \end{cases}$ |  |

$$y = [u] \Rightarrow y' = 0$$

تذکر: در نقطه ای که  $z \in z$  و تابع  $u$  در آن نقطه مینیمم نسبی داشته باشد آنگاه:

$$y = \left[ \sin \frac{3\pi}{2} \right] \frac{\sin \frac{3\pi}{2}}{} \rightarrow y' = 0$$

$$y = \left[ \sin \frac{\pi}{3} \right] \frac{\sin \frac{\pi}{3}}{\frac{\sqrt{3}}{2}} \notin z \rightarrow y' = 0$$

$$y = [\sin \pi] \frac{\sin \pi = 0 \in z}{\phi} \rightarrow y' = \phi$$