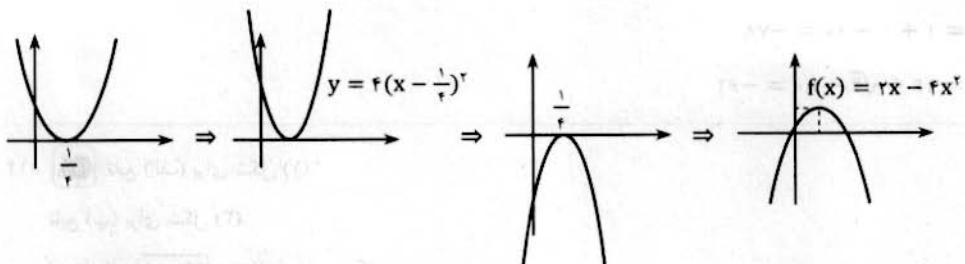
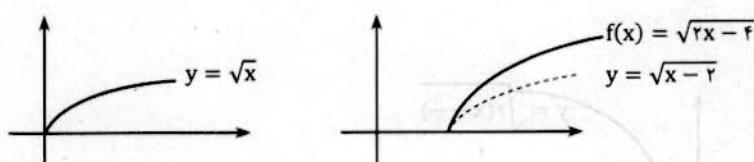


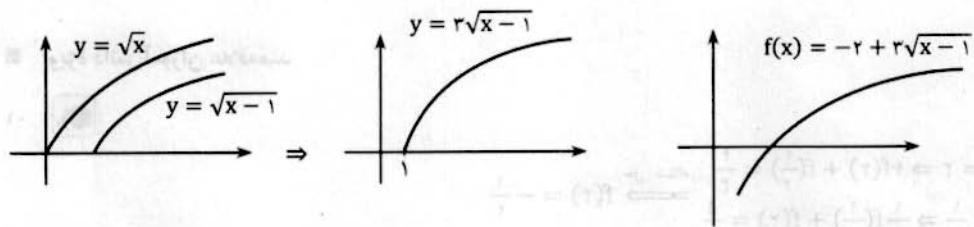
$$(الـ) f(x) = -r x^r + rx = -r\left(x^r - \frac{x}{r}\right) = -r\left(\left(x - \frac{1}{r}\right)^r - \frac{1}{r^r}\right) = -r\left(x - \frac{1}{r}\right)^r + \frac{1}{r}$$



$$\therefore f(x) = \sqrt{r(x-1)} = \sqrt{r} \sqrt{x-1}$$



$$\therefore f(x) = -1 + r\sqrt{x-1}$$



$$(الـ) \frac{f(x)-f(a)}{x-a} = \frac{\frac{rx-1}{x+r} - \frac{ra-1}{a+r}}{x-a} = \frac{\frac{(rx-1)(a+r) - (ra-1)(x+r)}{(x+r)(a+r)}}{x-a} = \frac{(rx-1)(a+r) - (ra-1)(x+r)}{(x+r)(a+r)(x-a)}$$

$$= \frac{rax + rx - a - r - (rax + ra - x - r)}{(x-a)(x+r)(a+r)} = \frac{rx - ra}{(x-a)(x+r)(a+r)} = \frac{r}{(x+r)(a+r)}$$

$$\therefore \frac{f(1+h)-f(1)}{h} = \frac{\frac{r(1+h)-1}{1+h+r} - \frac{r}{1+r}}{h} = \frac{r(1+h) - r - rh(r+1)}{rh(h+r)} = \frac{rh}{rh(h+r)} = \frac{r}{r+h+1}$$