



توازن انرژی و مواد

Dr Kharat

- Dimension and units:

$5m + 6kg = X \rightarrow$ Dimension is different

$5lb + 6kg = \checkmark \rightarrow$ Dimension is same but unit is different

- Dimension: is a property that can be measured, such as length, time, mass or temperature, or calculated by multiplying or dividing other dimension, such as: $\frac{\text{length}}{\text{time}} = \text{velocity}$, $(\text{length})^3 = \text{Volume}$.

- example: The position of an entity moving in a straight line along the X-axis depends on time (t) according to the following equation: $X(t) = at^2 - bt^3$ t(sec).

what are the dimension of a and b ?

$a \left(\frac{ft}{sec^2} \right)$ & $b \left(\frac{ft}{sec^3} \right)$

Reynolds Number: $Re = \frac{\rho V D}{\mu}$

if $\left\{ \begin{array}{l} \rho \left(\frac{gr}{cm^3} \right) \\ V \left(\frac{cm}{sec} \right) \\ D (cm) \end{array} \right.$

$\frac{gr}{cm^3} \cdot \frac{cm}{sec} \cdot \frac{cm}{cm} \equiv \frac{gr}{cm \cdot sec} = C.P (centi poise)$

density \rightarrow Velocity \rightarrow diameter \rightarrow viscosity \rightarrow ?

Note: Reynolds Number is Dimensionless

system	SI	CGS	AES
Length	meter (m)	centimeter (cm)	foot (ft)
mass	kilogram (kg)	gram (gr)	pound mass (lb _m) or (lb)
time	second (s)	second (s)	hour (hr)
Force	Newton (N)	dyne	pound force (lbf)

Field unit:

SCF = standard cubic foot }
 bbl = barrel (oil) }
 باسگاز }
 باریل }
 نفت

دو نوع بستر: 1. reservoir 2. Stock tank

رابطه دو بستر: $B_o \rightarrow_{oil} = 1.30 \frac{bbl \rightarrow_{reservoir}}{STB \rightarrow_{stock\ tank\ barrel}}$

$B_g \rightarrow_{gas} = 0.001 \frac{ft^3}{SCF}$

Note: 1 bbl = 5.61 ft³

Note: B_o: oil formation volume factor

unit conversion:

Note: $\overline{MW} \equiv x \left(\frac{lb_m}{lb_m\ mol} \right) \equiv x \left(\frac{gr}{gr\ mol} \right) \equiv x \left(\frac{kg}{kg\ mol} \right)$

example:

1000 $\frac{bbl}{day}$ (BPD) of oil flows through a 4 inch internal pipe. what is velocity in $\frac{m}{s}$?



$Q \left(\frac{volume}{time} \right) = \vec{V} \left(\frac{length}{time} \right) A (length)^2 \Rightarrow \vec{V} = \frac{Q}{A} = \frac{volumetric\ flow\ rate}{cross\ sectional}$

$1000 \frac{bbl}{day} \left| \frac{42\ gal}{bbl} \right| \frac{m^3}{264.17\ gal} \left| \frac{1\ day}{24\ hr} \right| \frac{1\ hr}{3600\ s} = 0.001840 \frac{m^3}{s}$

$A = \pi r^2 = \pi (2\ inch)^2 \left| \left(\frac{1\ m}{39.37\ inch} \right)^2 \right| = 0.00810\ m^2$

$\Rightarrow \vec{V} = 0.001840 \frac{m^3}{s} \left| \frac{1}{0.00810\ m^2} \right| = 0.227 \frac{m}{s}$

Dimensional Homogeneity:

1. All Additive terms on both side of the equation must have the same unit. $y = a + bx$

2. Exponents, transcendental functions, the arguments are dimensionless. In x^z , z is dimensionless, $Exp(x)$, $sin(x)$ too.

example: $t(\text{sec}) = t_0(?) + \frac{3.52(?) \text{ h(m)}^2}{V(\frac{\text{m}^3}{\text{sec}})}$

H-w

example: Darcy's Law: if $V(\frac{\text{cm}}{\text{s}})$ & $\mu(\text{cp})$ & $\frac{dP}{dX}(\frac{\text{atm}}{\text{cm}})$
 then $\Rightarrow K(\text{darcy}) \Rightarrow V = \frac{q}{A} = \frac{-K}{\mu} \frac{dP}{dX}$ (permeability)

1. if $V(\frac{\text{bbl}}{\text{day} \cdot \text{ft}^2})$ & $\frac{dP}{dX}(\frac{\text{Psi}}{\text{ft}})$ $\Rightarrow V = \frac{q}{A} = \frac{-1.128}{\mu} K \frac{dP}{dX}$ (viscosity)

2. if $V(\frac{\text{ft}}{\text{day}})$ & $\frac{dP}{dX}(\frac{\text{Psi}}{\text{ft}})$ $\Rightarrow V = \frac{q}{A} = \frac{6.33}{\mu} K \frac{dP}{dX}$ (prove?)

$K = -\mu V \frac{dX}{dP}$

$\Rightarrow (\text{cp}) (\frac{\text{cm}}{\text{s}}) (\frac{\text{cm}}{\text{atm}}) \left[\frac{1 \text{ m}^2}{100 \text{ cm}^2} \right] \left[\frac{3.2808 \text{ ft}}{1 \text{ m}} \right]^2 \left[\frac{60 \text{ s}}{1 \text{ min}} \right] \left[\frac{60 \text{ min}}{1 \text{ hr}} \right] \left[\frac{24 \text{ hr}}{1 \text{ day}} \right] \left[\frac{1 \text{ atm}}{14.696 \text{ Psi}} \right]$ evaluate?

$g_c \equiv \text{conversion factor} = \frac{6.33 (\text{cp}) \text{ ft}^2}{\text{Psi} \cdot \text{day}}$

$F = ma \rightarrow 1 \text{ lb}_f = (?) \text{ lb}_m \cdot \frac{\text{ft}}{\text{sec}^2}$

$\text{lb}_f = (1 \text{ lb}_m) \cdot 32.174 \frac{\text{ft}}{\text{sec}^2}$
 $\left(\frac{32.174 \text{ lb}_m \cdot \text{ft}^2}{\text{lb}_f \cdot \text{sec}^2} \right) \rightarrow g_c$ } $F = \frac{ma}{g_c}$

- in SI system:

$F(\text{N})$ & $m(\text{kg})$ & $a(\frac{\text{m}}{\text{sec}^2}) \Rightarrow g_c = 1 \frac{\text{kg} \cdot \text{m}}{\text{N} \cdot \text{sec}^2}$

- in CGS system:

$F(\text{dyne})$ & $m(\text{gr})$ & $a(\frac{\text{m}}{\text{sec}^2}) \Rightarrow g_c = 1 \frac{\text{kg} \cdot \text{m}}{\text{dyne} \cdot \text{sec}^2}$

✓ - in AFS system:

$F(\text{lb}_f)$ & $m(\text{lb}_m)$ & $a(\frac{\text{lb}_m}{\text{sec}^2}) \Rightarrow g_c = \boxed{32.174 \frac{\text{lb}_m \cdot \text{ft}}{\text{lb}_f \cdot \text{sec}^2}}$

example: find the kinetic Energy if (ft.lbf) of 200 lb_m moving at 5 $\frac{ft}{sec}$. $K_E = \frac{1}{2} m V^2$.

$$K_E \text{ (ft.lbf)} = \frac{1}{2} (200 \text{ lb}_m) (5 \frac{ft}{sec})^2 = 77.7 \text{ ft.lbf}$$

$32.174 \frac{lb_m \cdot ft}{lbf \cdot sec^2} g_c$

example: what is the potential Energy in (ft.lbf) of 45.4 kg drives hanging 20 ft above the surface of the earth?

$$P_E \text{ (ft.lbf)} = \frac{Mgh}{g_c}$$

$$P_E = \frac{45.4 \text{ kg} \left| \frac{lb_m}{0.454 \text{ kg}} \right| 32.178 \frac{ft}{sec^2} \left| 20 \text{ ft} \right.}{32.174 \frac{lb_m \cdot ft}{lbf \cdot sec^2} g_c} = 2000 \text{ ft.lbf}$$

significant figure:

$$65000 = 6.5 \times 10^4$$

$$0.00065 = 6.5 \times 10^{-4}$$

$$65000 \quad 2$$

$$65000. \quad 5$$

$$6.50 \times 10^4 \quad 3$$

$$(4.82) (2.653) = 12.78746$$

③ ④ 12.8 ③

Note: در ضرب و تقسیم کمترین مقدار را در نظر می گیریم.

$$110.3 \quad ④$$

$$0.038 \quad ④$$

$$110.338$$

$$110.3 \quad ④$$

Note: در جمع و تفریق بیشترین مقدار را در نظر می گیریم.

$$\text{Density} = \frac{\text{Mass}}{\text{Volume}} \Rightarrow \rho = \frac{m}{V}$$

$$\text{specific volume} = \frac{\text{Volume}}{\text{Mass}} \Rightarrow v = \frac{1}{\rho}$$

$\rho(T, P)$ for gas

$\rho(T)$ for liquid

$v(T, P)$ for gas

$v(T)$ for liquid

$$\text{specific gravity} = S.G. = \frac{\rho \rightarrow \text{substance}}{\rho_{ref} \rightarrow \text{Reference}}$$

$$\rho_{\text{substance}} = S.G \times \rho_{\text{ref}}$$

$$S.G = \frac{141.5}{131.5 + ^\circ\text{API}}$$

$$\text{or } ^\circ\text{API} = \frac{141.5}{S.G} - 131.5$$

Example: $\rho_{\text{water}}(4^\circ\text{C}) = 1.00 \frac{\text{gr}}{\text{cm}^3} = 1000 \frac{\text{kg}}{\text{m}^3} = 62.43 \frac{\text{lbm}}{\text{ft}^3}$

Example: Benzene:

$$S.G = 0.879 \left(\frac{20^\circ\text{C}}{4^\circ\text{C}} \right) \Rightarrow \rho_{(20^\circ\text{C})} = S.G \times \rho_{\text{water}}^{4^\circ\text{C}}$$

$$= (0.879)(62.43) = 54.9 \frac{\text{lbm}}{\text{ft}^3}$$

$$= (0.879)(1.00 \frac{\text{gr}}{\text{cm}^3}) = 0.879 \frac{\text{gr}}{\text{cm}^3}$$



<u>S.G</u>	<u>API</u>
0.9	25.7
0.85	35
0.80	45.32

نفت سنگینتر می شود

Note: نفت با کمتر از 20° API رانفت سنگینی است و بیشتر از 20° API سبک است.

Example: The density of a crude oil is 25° API. what is the specific gravity at 60°F referenced to water at 4°C?

$$S.G = \frac{141.5}{131.5 + ^\circ\text{API}} \Rightarrow \rho(60^\circ\text{F}) = (0.904)(0.999 \frac{\text{gr}}{\text{cm}^3}) = 0.903 \frac{\text{gr}}{\text{cm}^3}$$

$$\Rightarrow S.G = 0.904$$

Example: $S.G = 0.903 \left(\frac{60^\circ\text{F}}{4^\circ\text{C}} \right)$ & $\dot{V} = 400 (\text{bpd}) \left(\frac{\text{bbl}}{\text{day}} \right)$

& $\rho_{\text{water}}(4^\circ\text{C}) = 62.43 \frac{\text{lbm}}{\text{ft}^3}$

$$\dot{M} \left(\frac{\text{lbm}}{\text{min}} \right) = ? = 400 \frac{\text{bbl}}{\text{day}} \left| 0.903 \right| 62.43 \frac{\text{lbm}}{\text{ft}^3} \left| 5.615 \frac{\text{ft}^3}{1 \text{ bbl}} \right| \frac{1 \text{ day}}{24 \text{ hr}} \left| \frac{1 \text{ hr}}{60 \text{ min}} \right|$$

$$= 87.9 \frac{\text{lbm}}{\text{min}}$$

Mass fraction, Mole fraction, \overline{MW} , Basis

$$X_i = \text{mass fraction} = \frac{\text{weight of component} = \text{mass of component } i}{\text{mass of mixture} = \text{total mass}} \quad \sum_{i=1}^N X_i = 1$$

$$Y_i = \text{mole fraction} = \frac{\# \text{ mole of component} = \text{mole of component } i}{\text{Mole of mixture} = \text{total mole}} \quad \sum_{i=1}^N Y_i = 1$$

$$\textcircled{1} \overline{MW} = \text{Molecular weight} = \frac{\text{total mass}}{\text{total mole}}$$

$$\textcircled{2} \overline{MW} = Y_1 MW_1 + Y_2 MW_2 + \dots + Y_n MW_n = \sum_{i=1}^n Y_i MW_i$$

$$\textcircled{3} \frac{1}{\overline{MW}} = \frac{X_1}{MW_1} + \frac{X_2}{MW_2} + \frac{X_3}{MW_3} + \dots + \frac{X_n}{MW_n} = \sum_{i=1}^n \frac{X_i}{MW_i}$$

Example:

	Mass%	mass (lbm)	MW (lbm / lbm mol)	mole	% mole
C_1	62.6	62.6	16.04	3.903	78.4
C_2	21.42	21.42	30.07	0.7123	14.31
C_3	15.98	15.98	44.09	0.3624	7.28
Basis = 100 lbm	100%	100 lbm		4.978 mole	100%

$$\textcircled{1} \frac{\text{total mass}}{\text{total mole}} = \overline{MW} = 20.09 \frac{\text{lbm}}{\text{lbm mol}}$$

$$\textcircled{2} \sum_{i=1}^n Y_i MW_i = \overline{MW}$$

$$\textcircled{3} \sum_{i=1}^n \frac{X_i}{MW_i} = \frac{1}{\overline{MW}}$$

Temperature: principle temperature scale:

Relative: Absolute:

$^{\circ}\text{F}$ Fahrenheit $^{\circ}\text{R}$ Rankin

$^{\circ}\text{C}$ Celsius $^{\circ}\text{K}$ Kelvin (SI)

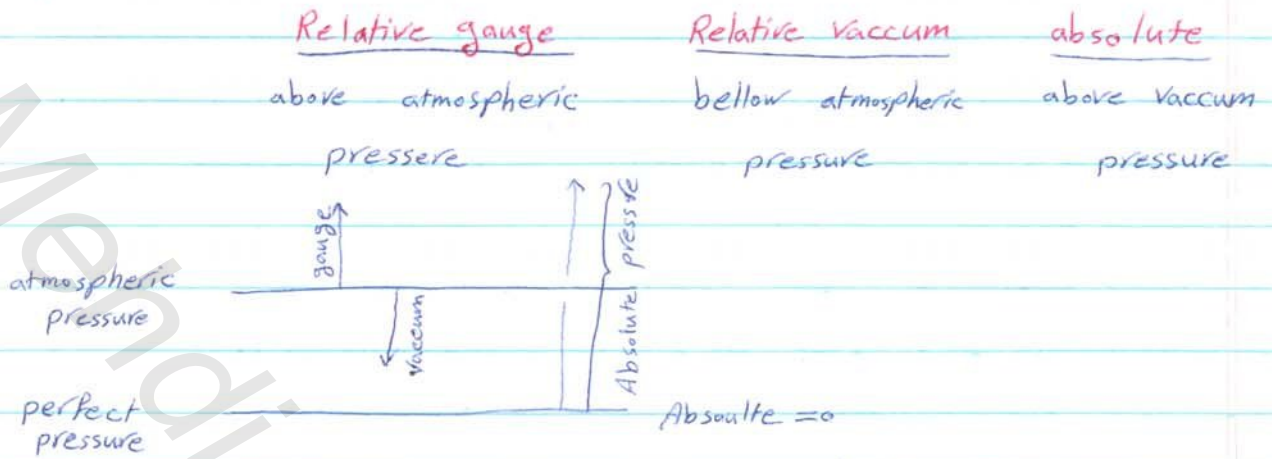
$$^{\circ}\text{R} = ^{\circ}\text{F} + 459.67$$

$$^{\circ}\text{K} = ^{\circ}\text{C} + 273.15$$

$$\frac{\Delta^{\circ}\text{F}}{\Delta^{\circ}\text{C}} = \frac{212^{\circ}\text{F} - 32^{\circ}\text{F}}{100^{\circ}\text{C} - 0^{\circ}\text{C}} = 1.8 \quad \frac{\Delta^{\circ}\text{F}}{\Delta^{\circ}\text{C}} = 1.8 \frac{^{\circ}\text{R}}{^{\circ}\text{K}} \quad ^{\circ}\text{R} = ^{\circ}\text{K}$$

$$T(^{\circ}\text{R}) = T(^{\circ}\text{K}) \cdot 1.8 \frac{^{\circ}\text{R}}{^{\circ}\text{K}}$$

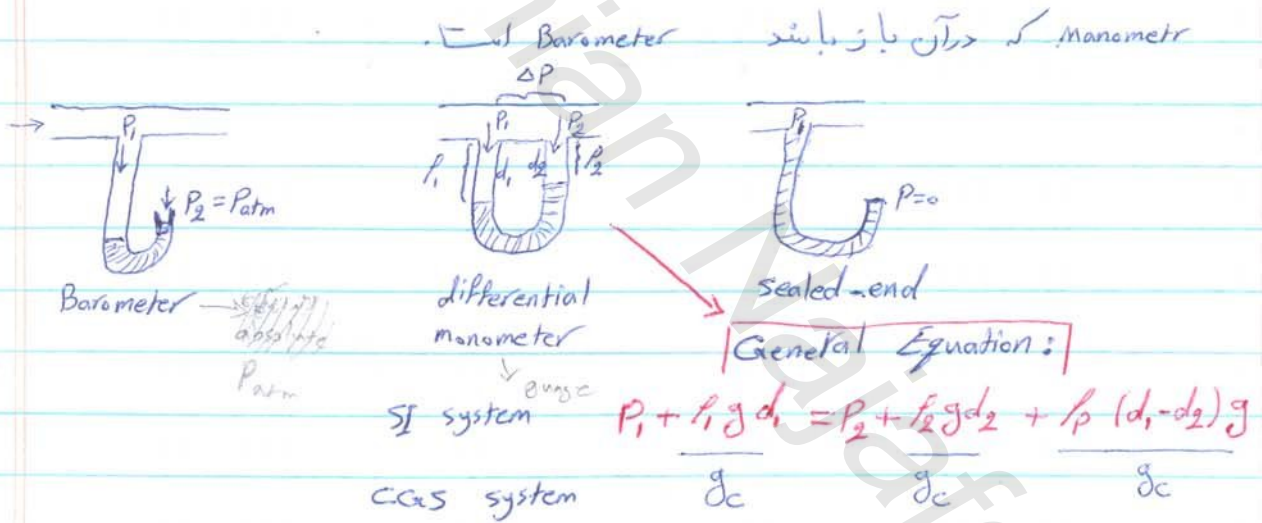
Pressure :



$$P_{abs} = P_{gauge} + P_{atm}$$

$$P_{abs} = P_{atm} - P_{vacuum}$$

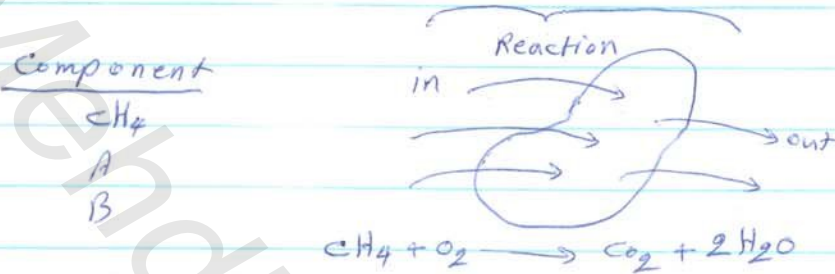
psia \rightarrow absolute
 psig \rightarrow gauge



Material Balance

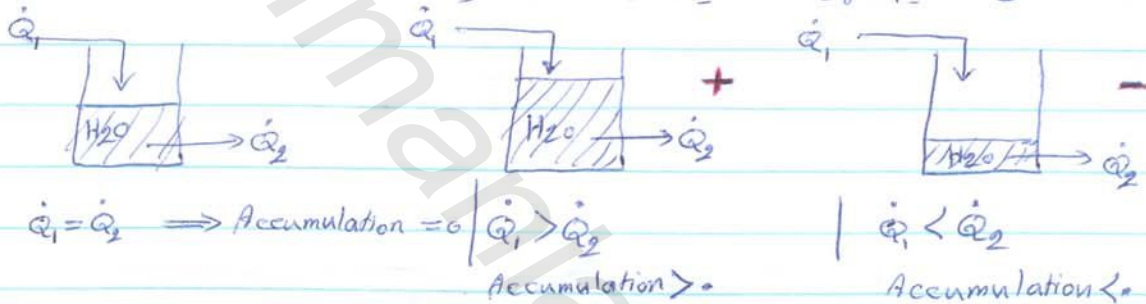
Hw: 6.4 - 6.6 - 7.1 - 7.3

is a computation method which accounts the material that enters, leaves is Generated, consumed, or accumulated within a system.



تغییرات در سیستم
accumulation

در حالتی که سیستم ناپایدار است یعنی سیستم با زمان تغییر کند.



steady state: No variation with time پایدار
unsteady state: variation with time ناپایدار

$$\text{Accumulation} = \text{Input} - \text{output} + \text{Generation} - \text{consumption}$$


steady state: $Acc = 0$
 $\Rightarrow In - out + Gen - Con = 0$

if No Reaction $\Rightarrow In - out = 0 \Rightarrow In = out$

- open system: ورودی و خروجی دارد.
- closed system: نه ورودی و نه خروجی
- semi-batch: یا ورودی دارد و خروجی ندارد و یا بالعکس

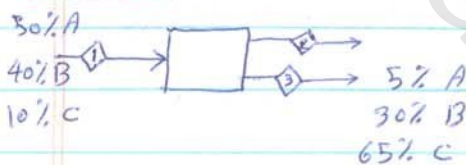
کاملترین سیستم: unsteady state
Reaction
open

step in material Balance :

1. understanding problem → 
2. Development of solution
3. Mathematical solution

solution of Material Balance problems :

1. **Sketch the process**. Make sure you understand the process and what questions are asked.
2. **label all streams**: This is an accounting step which assists in organizing a solution.
3. Include a **material balance table** with the sketch. Put all known compositions and flows in table. put all specifications on the sketch. This will clearly show what is unknowns.



Example

component	1	2	3
1-A	$X(1,1)$ 50%	$X(1,2)$	$X(1,3)$ 5%
2-B	$X(2,1)$ 40%	$X(2,2)$	$X(2,3)$ 30%
3-C	$X(3,1)$ 10%	$X(3,2)$	$X(3,3)$ 65%
total	S_1	S_2	S_3

bottom product stream = 60% Stream Feed specification

$X(I, J)$
↓
component Number

→ stream Number

: Amount of component I in stream J

$S_j = \text{Stream } j$

$M = \text{Total number of unknown} = (\text{Total number of stream}) \times (\text{Total number of component} + 1)$

مثال (در جدول فوق) : 3 $\times (3 + 1) = 12$

(مساكن unknown در جدول فوق)

$N = \text{Known} \Rightarrow M - N = \# \text{ Actual unknown}$

4. write the General Material balance equation.

5. Decide which terms apply in the specific case Address each of

the five terms. (Acc = In - out + Gen - Con)

6. write specific Material balance. تالیفات معین

7. Determine Maximum Number of unknown. #Stream (#comp + 1)

From this number subtract the known. that appear in the table to determine the actual unknown.

8. write independent equations equal in number to the number of unknowns. These equations include Material balance, specification, Definition and Basis. ارتباطی stream

9. solve the system of equation for all unknown.

↔ continue of Example:

Actual unknown = 6

① MB (Material Balance) = 3

② specification = 1

$$S_1 = 50\% S_1 + 40\% S_2 + 10\% S_3$$

$$S_2 = X(1,2) + X(2,2) + X(3,2)$$

③ Df = 1

④ Basis = 1

6

① Definition: $S_j = \sum_{I=1}^n X(I,j)$

check the solution: In = out ?

(برای مثال فقط) $S_1 = S_2 + S_3$

گونی به جدول
کامل برای
تست استواری
داده

Stream	①	②	③	④
Component	lbm/hr			
A				
B				
C				
D				
Total	S_1	S_2	S_3	S_4
T	T_1	T_2	T_3	T_4
P	P_1	P_2	P_3	P_4

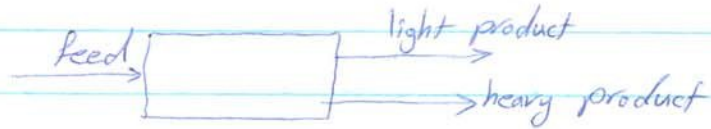
در این جدول واحد را
می نویسیم.

10. check \Rightarrow Total stream out = In برای وقتی که مادی
شیمیایی نداشته

Hw# 7.14 & 8.3 & 8.23

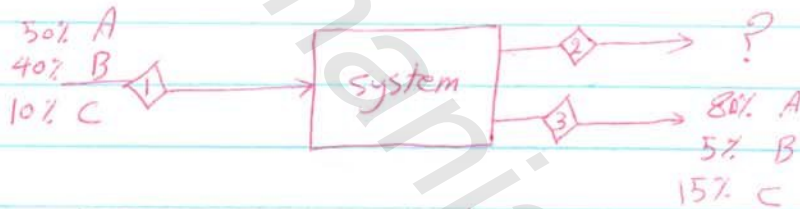
Eg: A separation process is shown below. A feed with 50% A, 40% B and 10% C enters the separator. Two streams, namely Light & Heavy products leaves the separator. The composition of the heavy stream is as follows:

80% A
5% B
15% C



Find the composition of light product stream if the ratio of the heavy to feed stream is 60%.

Sol:



comp	①	②	③
A	50%	X(1,2)	80%
B	40%	X(2,2)	5%
C	10%	X(3,2)	15%
total	S ₁	S ₂	S ₃

$$N = 3 \times (3+1) = 12$$

$$M = 6$$

Actual # of unknown = 6

$$MB = 3$$

$$DF = 1$$

$$SP = 1$$

$$\text{Basis} = 1$$

⑥

$$Acc = \dot{I}N - \dot{O}ut + G_{EN} - C_{EN}$$

$$\Rightarrow \boxed{IN = OUT}$$

Note: Steady state $\Rightarrow Acc = 0$

continue:

- 1- component A $X(1,2) + 0.8 S_3 = 0.5 S_1$ (1)
- 2- " B $X(2,2) + 0.05 S_3 = 0.4 S_1$ (2)
- 3- " C $X(3,2) + 0.15 S_3 = 0.1 S_1$ (3)
- 4- Definition $S_2 = X(1,2) + X(2,2) + X(3,2)$ (4)
- 5- specification $S_3 = 0.6 S_1$ (5)
- 6- Basis $S_1 = 100 \frac{kg}{hr}$ (6)

6	S_1
5	S_3
1	$X(1,2)$
2	$X(2,2)$
3	$X(3,2)$
4	S_2

comp	1	2	3
A	50%	25%	80%
B	40%	32.975%	5%
C	10%	12.5%	15%
total	100	40	60

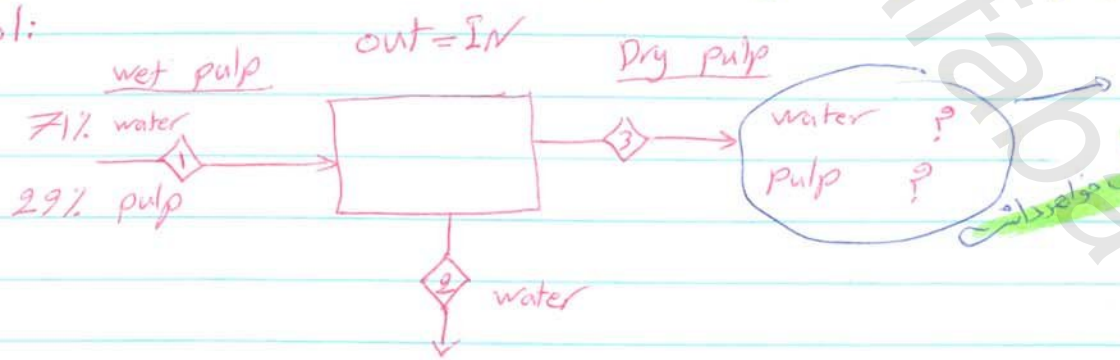
$X(1,2) = 2$
 $X(2,2) = 32$
 $X(3,2) = 1$
 $S_2 = 40$

check out = IN
 $40 + 60 = 100$ ✓

Eg: A wet paper pulp is found to contain 71% water. After drying it is found that 60% of the original water has removed. calculate the following:

- a) composition of the dried pulp.
- b) the mass of water removed per kilogram of wet pulp.

Sol:



اینطور
 باید
 در مقدار آب
 محاسبه داشت

comp	1	2	3
pulp	29%	0	$X(1,3)$
water	71%	100%	$X(2,3)$
total	S_1	S_2	S_3

$$N = 3(2+1) = 9$$

$$M = 4$$

$$\text{Actual unknown} = 5$$

MB	2
DF	1
SP	1
Basis	1
	5

$$\text{Acc} = \text{IN} - \text{out} + \text{GEN} - \text{CON}$$

S.S
N.R
N.R

$$\Rightarrow \text{out} = \text{IN}$$

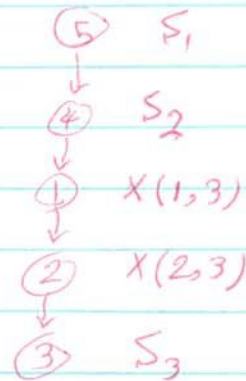
pulp: $X(1,3) = 0.29 S_1$ ①

water: $X(2,3) + S_2 = 0.71 S_1$ ②

Def: $S_3 = X(1,3) + X(2,3)$ ③

spi: $S_2 = 0.6(0.71 S_1)$ ④

Bas: $S_1 = 100$ ⑤



$$\Rightarrow S_1 = 100 \text{ Kg/hr}$$

$$S_2 = 42.6$$

$$X(1,3) = 29$$

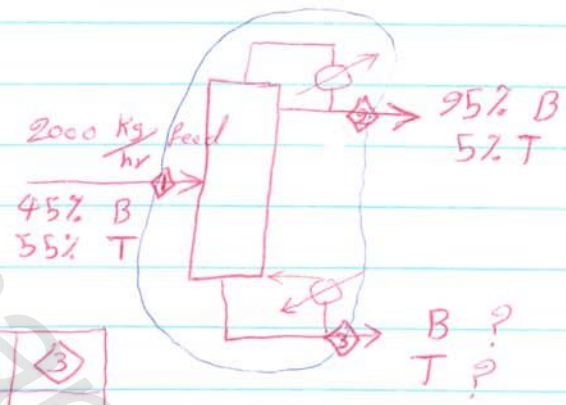
$$X(2,3) = 28.4$$

$$S_3 = 57.4$$

part (b) $\frac{42.6}{100}$

comp	①	②	③	part(a)
pulp	29	0	29	→ 50.5%
water	71	42.6	28.4	→ 49.5%
total	100	42.6	57.4	

Eg: A mixture containing 45% benzene (B) and 55% Toluene (T) by mass is feed to a distillation column. An overhead stream of 95% benzene is produced, and 8% of the benzene feed to the column leaves in the bottom stream. The feed rate is 2000 kg/hr. Determine the composition of the bottom stream.



Comp	①	②	③
B	45%	95%	$X(1,3)$
T	55%	5%	$X(2,3)$
total	2000	S_2	S_3

$$\begin{cases} N = 3(2+1) = 9 \\ M = 5 \\ \text{Actual unknown} = 4 \end{cases}$$

Steady state:
$$\overset{\circ}{A}c = \overset{\circ}{I}N - \overset{\circ}{O}ut + \underset{\text{No reaction}}{\overset{\circ}{G}en} - \overset{\circ}{C}on \Rightarrow \overset{\circ}{I}N = \overset{\circ}{O}ut$$

B: $X(1,3) + 0.95 S_2 = 900$ ①
 T: $X(2,3) + 0.05 S_2 = 1100$ ②
 Def: $S_3 = X(1,3) + X(2,3)$ ③
 Spe: $X(1,3) = 0.8 (900)$ ④



$\Rightarrow X(1,3) = 72$ & $X(2,3) = 1056.42$
 $S_2 = 871.58$ & $S_3 = 1128.42$

check: $\overset{\circ}{I}N = \overset{\circ}{O}ut \Rightarrow S_3 + S_2 = S_1$

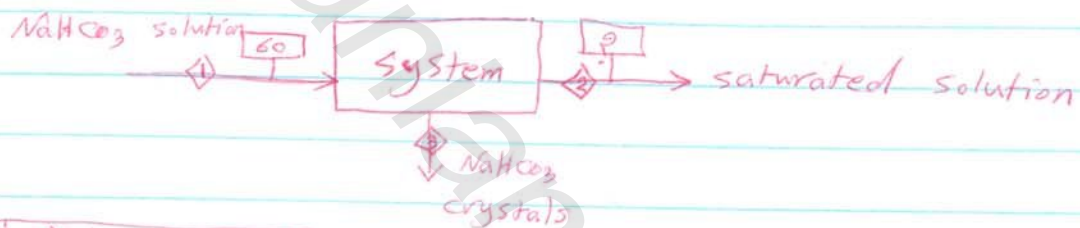
$1128.42 + 871.58 = 2000 \checkmark$

Eg: A tanks hold: 10,000 kg of saturated solution of NaHCO_3 at 60°C . we want to crystallize 500 kg of NaHCO_3 from the solution. To what Temperature must the solution be cooled?

Solubility

$T, ^\circ\text{C}$	$\frac{\text{Kg NaHCO}_3}{100 \text{ Kg H}_2\text{O}}$
60	16.4
50	14.45
40	12.7
30	11.1
20	9.6
10	8.14

sol:



Comp	①	②	③
NaHCO_3	$X(1,1)$ 1408.9	$X(1,2)$ 908.9	500
H_2O	$X(2,1)$ 8591.1	$X(2,2)$ 8591.9	0
total	10000	S_2	500

$$N = 9$$

$$M = 4$$

$$\text{Actual unknown} = 5$$

$$\text{MB} = 2$$

$$\text{Def} = 2$$

$$\text{Spec} = 1$$

$$5$$

$$X(1,1) = 10,000 \frac{\text{total}}{116.4} \times 16.4 \text{ Kg NaHCO}_3$$

$$X(2,1) = 10,000 - X(1,1)$$

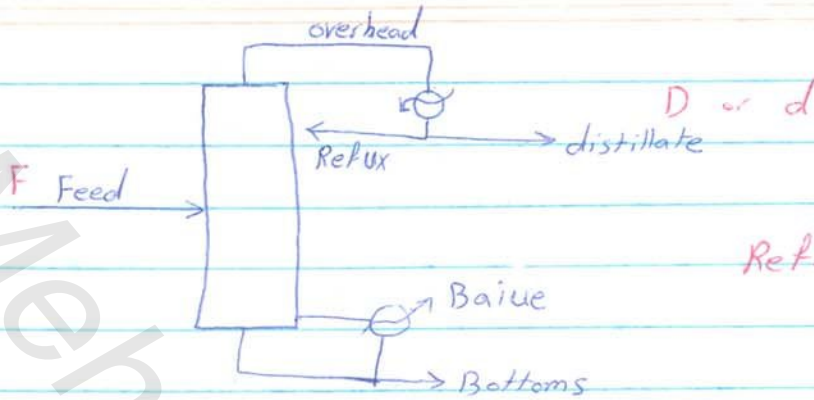
$$X(2,2) = X(2,1)$$

$$500 + X(1,2) = X(1,1)$$

$$S_2 = X(1,2) + X(2,2)$$

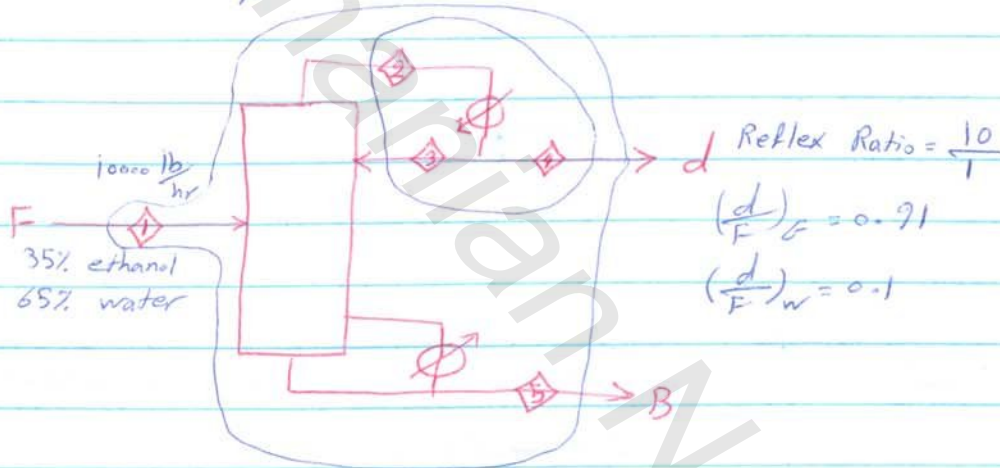
$$\Rightarrow \frac{\text{Kg NaHCO}_3}{100 \text{ Kg H}_2\text{O}} = \frac{908.9}{8591.9} \times 100 = 10.6 \frac{\text{Kg NaHCO}_3}{100 \text{ Kg H}_2\text{O}}$$

$$\Rightarrow \boxed{27^\circ\text{C}}$$



$$\text{Reflux Ratio} = \frac{\text{Reflux}}{\text{Distillate}}$$

Distillation column Example: 10,000 $\frac{\text{lb}}{\text{hr}}$ of an ethanol-water solution containing 35% ethanol are feed to a distillation tower. The Reflux Ratio is 10 to 1. The $\frac{d}{F}$ for ethanol is 0.91 and $\frac{d}{F}$ for water is 0.1. Determine material balance.



Comp	①	②	③	④	⑤
E	3500	$n(1,2)$	$n(1,3)$	$n(1,4)$	$n(1,5)$
W	6500	$n(2,2)$	$n(2,3)$	$n(2,4)$	$n(2,5)$
total	10000	S_2	S_3	S_4	S_5

$$M = 5(2+1) = 15$$

$$N = 3$$

$$\text{Actual unknowns} = 12$$



Ethanol ① $n(1,4) + n(1,5) = 3500$

water ② $n(2,4) + n(2,5) = 6500$

⑤ $S_2 = n(1,2) + n(2,2)$

⑦ $S_4 = n(1,4) + n(2,4)$



③ $n(1,4) + n(1,3) = n(1,2)$

④ $n(2,3) + n(2,4) = n(2,2)$

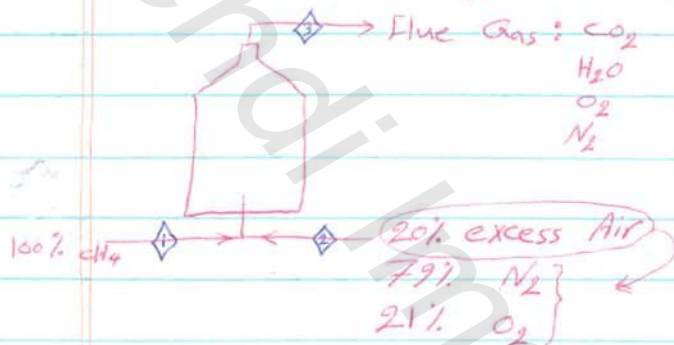
⑥ $S_3 = n(1,3) + n(2,2)$

⑧ $S_5 = n(1,5) + n(2,5)$

Material Balance with chemical Reaction:

Combustion:

Ex: ① methane is burned in a Furnace in the presence of 20% excess of Air. The reaction is complete. Find the composition of the Flue Gas on wet and dry basis.



Comp	①	②	③
CH ₄	100%	0	0
N ₂	0	79%	X(2,3)
O ₂	0	21%	X(3,3)
H ₂ O	0	0	X(4,3)
CO ₂	0	0	X(5,3)
total	S ₁	S ₂	S ₃

$$M = 3(5+1) = 18$$

$$N = 11$$

Actual unknown = 7

MB	4
DF	1
B	1
SP	1

Equation 7 ✓

$$\text{Out} = \text{IN} - \text{CON} + \text{GEN}$$

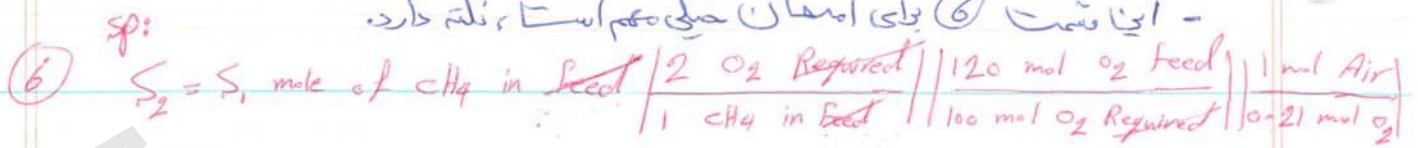
- ① N₂: X(2,3) = 0.79 S₂ Tie Component
- ② O₂: X(3,3) = 0.21 S₂ - S₁ mole CH₄ consumed

2 O ₂ consumed
1 CH ₄ consumed
- ③ H₂O: X(4,3) = S₁ mole CH₄ consumed

2 H ₂ O produce
1 CH ₄ consum
- ④ CO₂: X(5,3) = S₁ mole CH₄ consumed

1 CO ₂ produce
1 CH ₄ consum
- ⑤ S₃ = X(2,3) + X(3,3) + X(4,3) + X(5,3)

- این مثال برای امتحان خلیج فارس است و نکته دارد.



(Note: 20% excess $O_2 \rightarrow \frac{120 \text{ mole feed}}{100 \text{ mole Required}}$)

$\left\{ \begin{array}{l} O_2 \text{ Required} \\ \% \text{ excess} \end{array} \right\} \left\{ 21\% \text{ O}_2 \text{ in Air} \right\}$

Boisr



$\Rightarrow S_2 = 1142.8 \quad X(2,3) = 902.8 \quad X(3,3) = 39.98$
 $X(4,3) = 200 \quad X(5,3) = 100 \quad S_3 = 1242.78$

comp	①	②	③	wet Analysis	orsat/Dry Analysis آب، اسفندی لیم
CH ₄	100%	0	0	0	0
N ₂	0	79%	902.8	72.6%	86.6% → 902.8
O ₂	0	21%	39.98	3.2%	3.8% → 39.98
H ₂ O	0	0	200	16.1%	0 → 0
CO ₂	0	0	100	8.1%	9.6% → 100
total	100	1142.8	1242.78	100%	100% → 1042.78

EX(2): pervious example with 50% Conversion:

comp	①	②	③	
CH ₄	100%	0	X(1,3)	MB = 5
N ₂	0	79%	X(2,3)	DF = 1
O ₂	0	21%	X(3,3)	Sp = 1
H ₂ O	0	0	X(4,3)	Bar = 1
CO ₂	0	0	X(5,3)	8
total	S ₁	S ₂	S ₃	

unknown = 8

$$\text{Out} = \sum N - \text{CoN} + \text{Gen}$$

$$\text{CH}_4: X(1,3) = S_1 - S_1 \text{ mole CH}_4 \text{ feed} \left| \frac{50 \text{ mole CH}_4 \text{ consum}}{100 \text{ mole CH}_4 \text{ feed}} \right|$$

$$\text{N}_2: X(2,3) = 0.79 S_2$$

$$\text{O}_2: X(3,3) = 0.21 S_2 - S_1 \text{ mole CH}_4 \text{ f} \left| \frac{50 \text{ mol CH}_4 \text{ con}}{100 \text{ mol CH}_4 \text{ f}} \right| \left| \frac{2 \text{ mol O}_2 \text{ con}}{1 \text{ mol CH}_4 \text{ con}} \right|$$

$$\text{H}_2\text{O}: X(4,3) = S_1 \text{ mole CH}_4 \text{ f} \left| \frac{50 \text{ mol CH}_4 \text{ con}}{100 \text{ mol CH}_4 \text{ F}} \right| \left| \frac{2 \text{ mol H}_2\text{O Gen}}{1 \text{ CH}_4 \text{ con}} \right|$$

$$\text{CO}_2: X(5,3) = S_1 \text{ mole CH}_4 \text{ f} \left| \frac{50 \text{ mol CH}_4 \text{ con}}{100 \text{ mol CH}_4 \text{ f}} \right| \left| \frac{1 \text{ mol CO}_2 \text{ Gen}}{1 \text{ mol CH}_4 \text{ con}} \right|$$

$$S_3 = X(1,3) + X(2,3) + X(3,3) + X(4,3) + X(5,3)$$

$$S_2 = S_1 \text{ mole CH}_4 \text{ feed} \left| \frac{2 \text{ mol O}_2 \text{ Required}}{1 \text{ mol CH}_4 \text{ Feed}} \right| \left| \frac{120 \text{ mol O}_2 \text{ F}}{100 \text{ mol O}_2 \text{ Required}} \right| \left| \frac{1 \text{ mol Air}}{0.21 \text{ mol O}_2} \right|$$

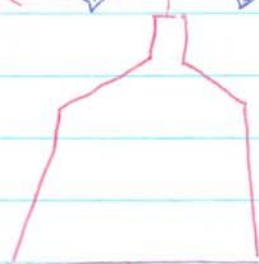
$$S_1 = 100$$

comp	1	2	3	wet analysis
CH ₄	100%	0	50	4%
N ₂	0	79%	902.8	72.6%
O ₂	0	21%	140	11.3%
H ₂ O	0	0	100	8%
CO ₂	0	0	50	4%
total	100		1242.8	100%

total

Ex ③: A Furnace burns C₃H₈. The orsat analysis of the combustion Gases is N₂: 83.8%, O₂: 5.5%, CO₂: 8.6%, and CO: 2.1%. what was the percentage excess Air?

H₂O ← 4 → 3 →



N₂ 83.8%
O₂ 5.5%
CO₂ 8.6%
CO 2.1%

نظرة: و النتیج
ورسات
ولی اینجی نیست و باید بدینک بفار
آب در خروجی وجود دارد

100% C₃H₈

Air excess?

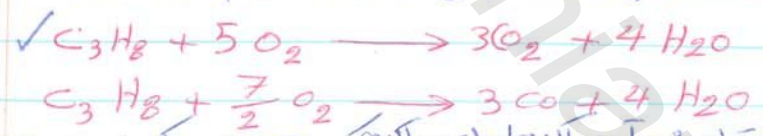
* ممکن است در Ex 3 سوال شود. oraset را به wet analy تبدیل کنیم.

Comp	1	2	3	4
C ₃ H ₈	100%	0	0	0
N ₂	0	79%	X(2,3) 83.8%	0
O ₂	0	21%	X(3,3) 5.5%	0
CO ₂	0	0	X(4,3) 8.6%	0
CO	0	0	X(5,3) 2.1%	0
H ₂ O	0	0	0	100%
total	S ₁	S ₂	S ₃	S ₄

4 unknown

$$out = IN - CoN + GEN$$

نکته: در مسائلی که composition خروجی را داشته باشیم می توانیم خروجی را به عنوان Basis انتخاب کنیم.



نکته: در سوختی هیدروکربنی همیشه وقتی CO تولید شود آن والنتی اصلی و والنتی که CO تولید می کند فرعی است.

$$S_3 = 100 \text{ mole}$$

$$N_2: out = IN \quad 83.8 = 0.79 S_2 \Rightarrow S_2$$

$$C_3H_8: out = IN - CoN + GEN \Rightarrow IN = CoN$$

$$\Rightarrow S_1 = 8.6 \text{ mol } CO_2 \left| \frac{1 \text{ } C_3H_8}{3 \text{ } CO_2} \right| + 2.1 \text{ mole } CO \left| \frac{1 \text{ mol } C_3H_8}{3 \text{ mol } CO} \right|$$

$$* H_2O: out = GEN \quad S_4 = 8.6 \text{ mol } CO_2 \left| \frac{4 \text{ } H_2O}{3 \text{ } CO_2} \right| + 2.1 \text{ mole } CO \left| \frac{4 \text{ } H_2O}{3 \text{ } CO} \right|$$

$$\Rightarrow S_1 = 3.57 \quad S_2 = 106.1 \quad S_4 = 14.3$$

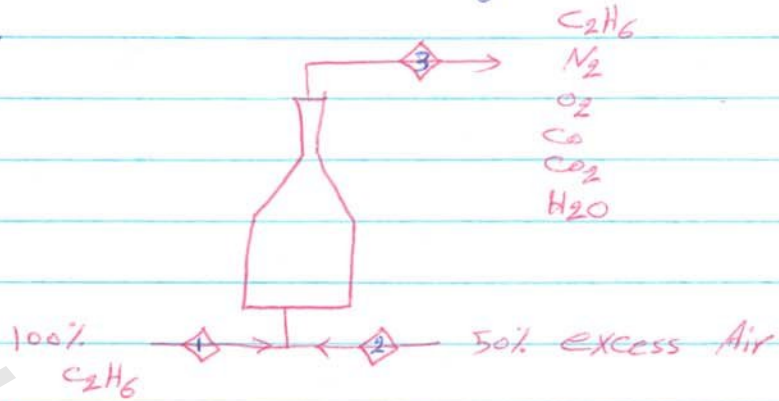
$$\% \text{ excess } O_2 = \frac{\text{Feed } O_2 - \text{Required } O_2}{\text{Required } O_2} \times 100$$

نکته: در مسائل فنی فقط برای والنتی اصلی است یعنی برای والنتی CO نوشته نمی شود.

$$\% \text{ excess } = \frac{(0.21)(106.1) - 3.57 \text{ mol } C_3H_8 \left| \frac{5 \text{ mol } O_2}{1 \text{ } C_3H_8} \right|}{3.57 \text{ mol } C_3H_8 \left| \frac{5 \text{ mol } O_2}{1 \text{ } C_3H_8} \right|} \times 100 = 24.6\%$$

Ex(5): Combustion C_2H_6 with 50% excess Air

conversion: 90% → 25% of that burns goes to CO and the balance to CO_2 .



comp	1	2	3
C_2H_6	100%	0	$X(1,3)$
O_2	0	21%	$X(2,3)$
N_2	0	79%	$X(3,3)$
CO_2	0	0	$X(4,3)$
CO	0	0	$X(5,3)$
H_2O	0	0	$X(6,3)$
total	S_1	S_2	S_3



Outs = IN - CON + GEN

9 unknown (6 MB, 1 D, 1 sp, 1 B)

$$C_2H_6: X(1,3) = S_1 - S_1 \text{ mol } C_2H_6 \left| \frac{0.9 C_2H_6 \text{ con}}{1 C_2H_6 F} \right.$$

$$O_2: X(2,3) = 0.21 S_2 - S_1 \text{ mol } C_2H_6 \times \frac{0.7 C_2H_6 \text{ con}}{1 C_2H_6 F} \left\{ \begin{array}{l} \text{Reaction \# 1} \\ 0.75 \text{ mol } C_2H_6 \left| \frac{7 O_2}{2} \right. \\ 1 \text{ mol } C_2H_6 \left| 1 C_2H_6 \right. \end{array} \right.$$

$$\left. \begin{array}{l} 0.25 \text{ mol } C_2H_6 \left| \frac{5 O_2}{2} \right. \\ 1 \text{ mol } C_2H_6 \left| 1 C_2H_6 \right. \end{array} \right\}$$

Reaction # 2

$$N_2: X(3,3) = 0.79 S_2$$

$$CO_2: X(4,3) = 0.9 S_1 (0.75) \text{ mole } C_2H_6 \text{ consumed in React\#1} \left| \begin{array}{l} 2 \text{ mol } CO_2 \\ 1 C_2H_6 \end{array} \right|$$

$$CO: X(5,3) = 0.9 S_1 (0.25) \text{ mole } C_2H_6 \text{ consumed in React\#2} \left| \begin{array}{l} 2 \text{ mol } CO \\ 1 C_2H_6 \end{array} \right|$$

$$H_2O: X(6,3) = 0.9 S_1 \text{ mole } C_2H_6 \left| \begin{array}{l} 3 \text{ mole } H_2O \\ 1 C_2H_6 \end{array} \right|$$

$$S_3 = X(1,3) + X(2,3) + X(3,3) + X(4,3) + X(5,3) + X(6,3)$$

$$S_2 = \left\{ \begin{array}{l} O_2 \text{ Required} \\ 150 O_2 \text{ Feed} \\ 100 O_2 \text{ Required} \end{array} \right\} \left| \begin{array}{l} 1 \text{ Air} \\ 0.21 O_2 \end{array} \right|$$

Note: $S_2 = \left\{ \begin{array}{l} O_2 \text{ Required} \\ \% \text{ excess} \\ \% O_2 \text{ in Air} \end{array} \right\}$

$$S_2 = \text{mole } \left\{ \begin{array}{l} C_2H_6 \\ S_1 \end{array} \right\} \left| \begin{array}{l} 7/2 O_2 \text{ Required} \\ 150 \\ 100 \end{array} \right| \left| \begin{array}{l} 1 \\ 0.21 \end{array} \right|$$

نکته: در اینجا (O_2) فقط باید (و البته اصلی را در نظر بگیریم)

$$S_1 = 100$$

$$\Rightarrow S_2 = 250.0 \quad X(1,3) = 10 \quad X(2,3) = 232.5$$

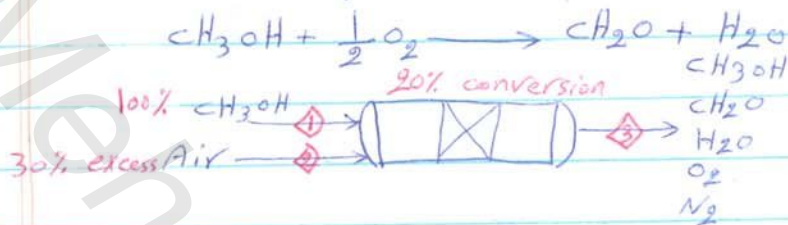
$$X(3,3) = 197.5 \quad X(4,3) = 135 \quad X(5,3) = 45$$

$$X(6,3) = 270 \quad S_3 = 2667.5$$

Hw # 7 chapter 9, chapter 10
 27, 29 13, 19

Recycle: calculation:

Ex: consider the production of formaldehyde from methanol.



suppose that the percentage conversion is 20% of the methanol at 30% excess Air. Find the composition of the product:

comp	1	2	3	
CH ₃ OH	100%	0	X(1,3)80	Acc = IN - out + GEN - CoN
N ₂	0	79%	X(2,3)244.5	→ out = IN + GEN - CoN
O ₂	0	21%	X(3,3)55	8 unknown
CH ₂ O	0	0	X(4,3)20	5 MB
H ₂ O	0	0	X(5,3)20	1 SP
total	S ₁	S ₂	S ₃	1 D 1 B

$$\begin{aligned} \text{CH}_3\text{OH} : & \quad X(1,3) = S_1 - \frac{20}{100} S_1 \\ \text{N}_2 : & \quad X(2,3) = 0.79 S_2 \\ \text{O}_2 : & \quad X(3,3) = 0.21 S_2 - \frac{20}{100} S_1 \text{CH}_3\text{OH} \left| \frac{1}{2} \text{O}_2 \right| \\ \text{CH}_2\text{O} : & \quad X(4,3) = \frac{20}{100} S_1 \text{CH}_3\text{OH} \left| \frac{1}{1} \text{CH}_2\text{O} \right| \\ \text{H}_2\text{O} : & \quad X(5,3) = \frac{20}{100} S_1 \text{CH}_3\text{OH} \left| \frac{1}{1} \text{H}_2\text{O} \right| \end{aligned}$$

$$S_2 = \left\{ \text{O}_2 \text{ Required} \right\} \left\{ \frac{130 \text{ O}_2 \text{ F}}{100 \text{ O}_2 \text{ Required}} \right\} \left\{ \frac{1 \text{ Air}}{0.21 \text{ O}_2 \text{ F}} \right\} \Rightarrow$$

$$S_2 = S_1 \text{ Mole CH}_3\text{OH} \left| \frac{1}{1} \text{CH}_3\text{OH} \right| \left| \frac{1}{100} \right| \left| \frac{1}{0.21} \right|$$

$$S_3 = X(1,3) + X(2,3) + X(3,3) + X(4,3) + X(5,3)$$

$\Rightarrow S_1 = 100 \text{ Mole}$

$S_2 = 309.52$

$X(1,3) = 80$

$X(2,3) = 244.52$

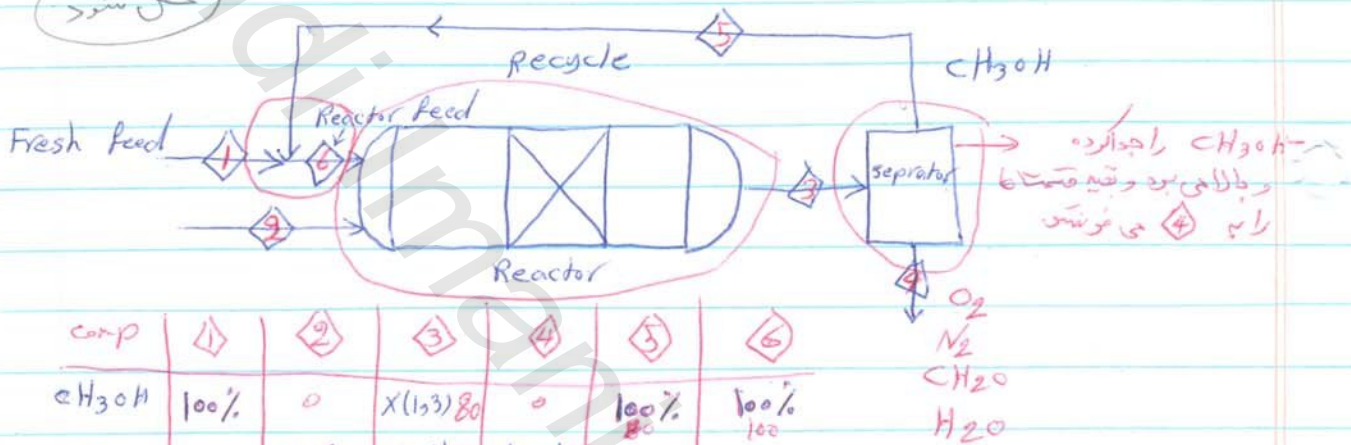
$X(3,3) = 55$

$X(4,3) = 20$

$X(5,3) = 20$

Ex: در موازنه باطل کنید + صورت مسئله

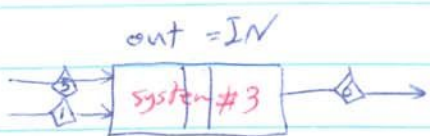
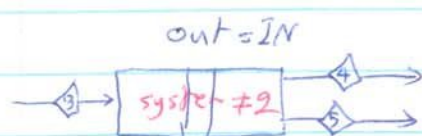
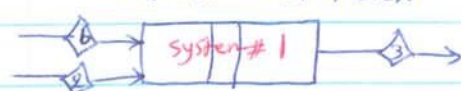
حل کنید



CH₃OH اجزای جدا شده و باقی مانده است
این 4 می فرستد

comp	1	2	3	4	5	6
CH ₃ OH	100%	0	X(1,3) 80	0	100%	100%
O ₂	0	21% 65	X(2,3) 55	X(2,4) 55	0	0
N ₂	0	79% 244.5	X(3,3) 244.5	X(3,4) 244.5	0	0
CH ₂ O	0	0	X(4,3) 20	X(4,4) 20	0	0
H ₂ O	0	0	X(5,3) 20	X(5,4) 20	0	0
total	S ₁ 20	S ₂ 309.5	S ₃ 419.5	S ₄ 337.5	S ₅ 80	S ₆ 100

نکته: می توانیم نوشتن موازنه را با توجه به system و component نوشت
 $out = IN - C_o N + C_{in} N$
 Component



$$\text{CH}_3\text{OH}: \#1 X(1,3) = S_6 - \frac{20}{100} S_6 \quad (1)$$

$$\#2 X(1,5) = X(1,3) \quad S_5$$

$$\#3 X(1,6) = X(1,5) + S_1 \quad S_6 \quad S_5$$

$$\text{O}_2: \#4 X(2,3) = 0.21 S_2 - \frac{20}{100} S_6 \left| \frac{1}{2} \text{O}_2 \right| \quad (2)$$

$$\#5 X(2,4) = X(2,3)$$

$$\text{N}_2: \#6 X(3,3) = 0.79 S_2$$

$$\#7 X(3,4) = X(3,3)$$

$$\text{CH}_2\text{O}: \#8 X(4,3) = \frac{20}{100} S_6 \left| \begin{array}{c} \text{CH}_3\text{OH} \\ 1 \text{CH}_2\text{O} \\ 1 \text{CH}_3\text{OH} \end{array} \right| \quad (3)$$

$$\#9 X(4,4) = X(4,3)$$

$$\text{H}_2\text{O}: \#10 X(5,3) = \frac{20}{100} S_6 \left| \begin{array}{c} \text{CH}_3\text{OH} \\ 1 \text{H}_2\text{O} \\ 1 \text{CH}_3\text{OH} \end{array} \right| \quad (4)$$

$$\#11 X(5,4) = X(5,3)$$

$$\text{Def: } \#12 S_3 = X(1,3) + X(2,3) + X(3,3) + X(4,3) + X(5,3) \quad (7)$$

$$\#13 S_4 = X(2,4) + X(3,4) + X(4,4) + X(5,4)$$

$$\text{sp: } \#14 S_2 = S_6 \left| \begin{array}{c} \text{CH}_3\text{OH} \\ \frac{1}{2} \text{O}_2 \\ 1 \text{CH}_3\text{OH} \end{array} \right| \left| \begin{array}{c} 1.3 \\ 1 \\ 0.21 \end{array} \right| \quad (5)$$

$$\text{Bas: } \#15 S_6 = 100 \text{ mole} \quad (6)$$

Ex:

Formaldehyde is manufactured by catalytic oxidation of methanol using an excess of Air.



A secondary, undesirable reaction occurs if conditions are not properly controlled to form Formic Acid.

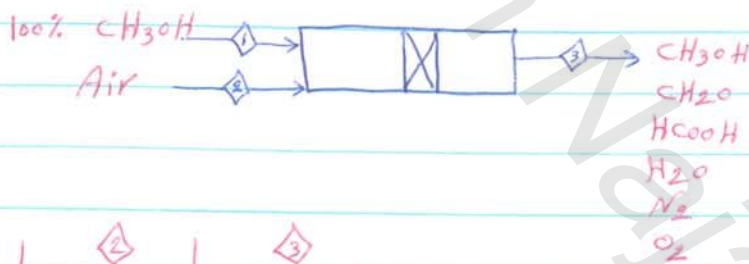


The product stream have the following composition.

component	mole %
CH ₃ OH	8.6
CH ₂ O	3.1
HCOOH	0.6
H ₂ O	3.7
O ₂	16
N ₂	68

Find:

- conversion of CH₃OH to CH₂O.
- % excess Air.
- Molar ratio of Methanol to Air.



comp	①	②	③
CH ₃ OH	100%	0	8.6
CH ₂ O	0	0	3.1
HCOOH	0	0	0.6
H ₂ O	0	0	3.7
O ₂	0	21%	16
N ₂	0	79%	68
total	S ₁ 12.3	S ₂ 86.1	100

$$S_3 = 100 \text{ mole}$$

$$N_2: 0.79 S_2 = 68$$

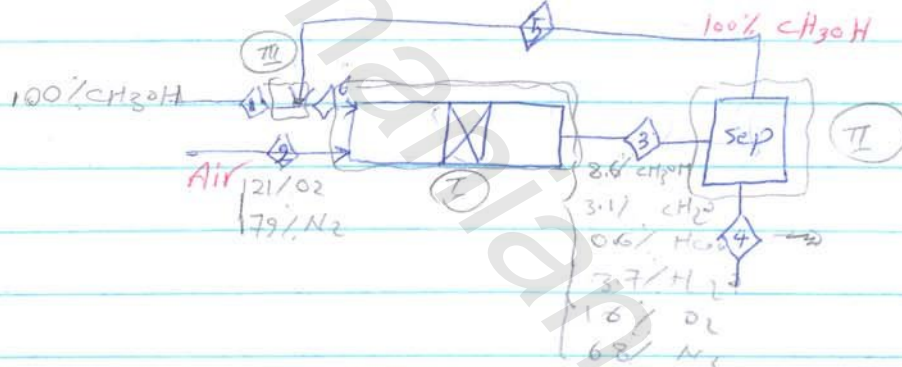
$$CH_3OH: \left\{ \begin{array}{l} 8.6 \text{ mol } CH_3OH = S_1 - \left(3.1 \text{ mol } CH_2O \left| \frac{1 CH_3OH}{1 CH_2O} \right. \right) + 0.6 \text{ mol } HCOOH \\ \left. \left| \frac{1 CH_2O}{HCOOH} \right| \left| \frac{1 CH_3OH}{1 CH_2O} \right| \right) \end{array} \right.$$

$$8.6 \text{ mol } CH_3OH = S_1 - 3.7 \text{ mol } H_2O \left| \frac{1 CH_3OH}{1 H_2O} \right|$$

$$\% \text{ Excess} = 194\%$$

EX: Homeworks

اگر مثال قبلی را با separator دانسته باشیم



عن	1	2	3	4	5	6
CH ₃ OH	100%	0	8.6%	0	100%	10%
CH ₂ O	0	0	3.1%	7(2,4)	0	0
HCOOH	0	0	0.6%	2(3,4)	0	0
H ₂ O	0	0	3.7%	2(4,4)	0	0
O ₂	0	21%	16%	2(5,4)	0	0
N ₂	0	79%	68%	2(6,4)	0	0
Total	S ₁	S ₂	S ₃	S ₂	S ₅	S ₆

$$\text{un24 } N_2 = 6(7) - 31 = 11$$

Element Balance:

Ex: Dehydro generation of 100 mole Ethane in a steady state reactor $C_2H_6 \rightarrow C_2H_4 + H_2$.

The product stream is analyzed for H_2 and it is found that the molar flow rate is 40 mol/min .

Find the composition of the product.



Comp	In	Out	
C_2H_6	100	$X(1,2) 60$	42.8%
C_2H_4	0	$X(2,2) 40$	28.6%
H_2	0	40	28.6%
Total	100	$\Sigma 140$	

$$\text{out} = \text{IN}$$

$$C: X(1,2) \text{ mol } C_2H_6 \left| \frac{2 \text{ mol } C}{1 \text{ mol } C_2H_6} \right| + X(2,2) \text{ mol } C_2H_4 \left| \frac{2 \text{ mol } C}{1 \text{ mol } C_2H_4} \right|$$

$$= 100 \text{ mol } C_2H_6 \left| \frac{2 \text{ mol } C}{1 \text{ mol } C_2H_6} \right| \Rightarrow X(1,2) + X(2,2) = 100$$

$$H: X(1,2) \text{ mol } C_2H_6 \left| \frac{6 \text{ mol } H}{1 \text{ mol } C_2H_6} \right| + X(2,2) \text{ mol } C_2H_4 \left| \frac{4 \text{ mol } H}{1 \text{ mol } C_2H_4} \right|$$

$$+ 40 \text{ mol } H_2 \left| \frac{2 \text{ mol } H}{1 \text{ mol } H_2} \right| = 100 \text{ mol } C_2H_6 \left| \frac{6 \text{ mol } H}{1 \text{ mol } C_2H_6} \right|$$

$$\Rightarrow 1.5X(1,2) + X(2,2) = 130$$

$$\Rightarrow X(1,2) = 60 \quad , \quad X(2,2) = 40$$

HW: methane is fed to a furnace to burn with 100% excess air. The outlet O_2 was found to be 220 mole based on 100 mol of methane. Find the composition of product.



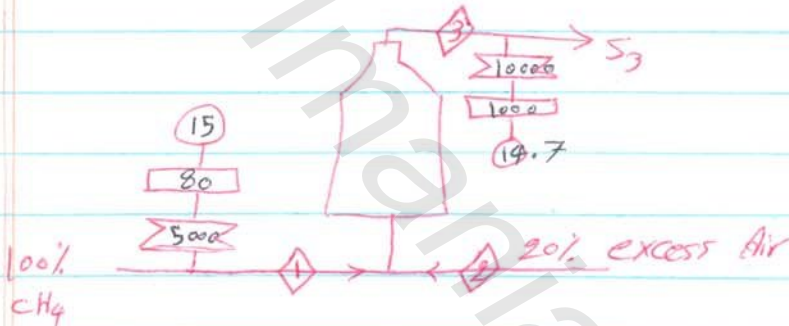
ideal
 $P\dot{V} = \dot{n}RT$

real
 $P\dot{V} = \sum \dot{n}_i RT$

مثال

مثال انعام از حالت ایدال

Ex: Flue Gas at 1000°F and 14.7 psi leave Furnace at a volumetric rate of 10,000 CFM. The meter on the fuel feed indicates a rate of 5000 CFM at 80°F and 15 psi. If combustion is complete with 20% excess Air, are the two meters consistent?



$$P\dot{V} = \dot{n}RT$$

comp	1	2	3
CH ₄	100%	0	0
N ₂	0	79%	X(2,3)
O ₂	0	21%	X(3,3)
H ₂ O	0	0	X(4,3)
CO ₂	0	0	X(5,3)
	S ₁	S ₂	S ₃

$$P_1 \dot{V}_1 = S_1 RT_1$$

$$\& P_3 \dot{V}_3 = S_3 RT_3$$

↓
 ؟ = ✓ ← با 10000 مقارنه

$$S_1 = \frac{P_1 \dot{V}_1}{RT_1} = \frac{(15 \text{ psi}) (5000 \frac{\text{ft}^3}{\text{min}})}{10.731 \frac{\text{ft}^3 \text{ lbf}}{\text{lbmol R}} (80 + 460) \text{ R}} = 12.95 \frac{\text{lbmol}}{\text{min}}$$

$$\text{out} = \sum N - \text{con} + \text{Gen}$$

$$X(2,3) = 0.79 S_2 = \boxed{116.92}$$

$$S_2 = 12.95 \text{ mol CH}_4 \left| \begin{array}{l} 2 \text{ O}_2 \\ 1 \text{ CH}_4 \end{array} \right| \frac{120 \text{ mol O}_2 \text{ P}}{100 \text{ mol O}_2 \text{ R}} \left| \text{Air} \right| 0.21 \text{ O}_2$$

$$X(3,3) = 0.21 S_2 - 12.95 \text{ mol CH}_4 \left| \begin{array}{l} 2 \text{ O}_2 \\ 1 \text{ CH}_4 \end{array} \right| = \boxed{5.18}$$

$$X(4,3) = 12.95 \text{ mol CH}_4 \left| \begin{array}{l} 2 \text{ H}_2\text{O} \\ 1 \text{ CH}_4 \end{array} \right| = \boxed{25.9}$$

$$X(5,3) = 12.95 \text{ mol CH}_4 \left| \begin{array}{l} 1 \text{ CO}_2 \\ 1 \text{ CH}_4 \end{array} \right| = \boxed{12.95}$$

$$S_3 = X(2,3) + X(3,3) + X(4,3) + X(5,3)$$

$$S_3 = 160.95 \frac{\text{mol}}{\text{min}}$$

$$P_3 \dot{V}_3 = S_3 R T_3 \quad \rightarrow \quad \dot{V}_3 = \frac{S_3 R T_3}{P_3} = \frac{(160.95)(1000 + 460)(0.73)}{14.7}$$

$$\rightarrow \boxed{\dot{V}_3 = 171500 \frac{\text{ft}^3}{\text{min}}} \rightarrow \text{دسته قراب است}$$

Energy Balance

Accounting for the energy that flows across the system boundaries or accumulates within the system.

\hat{E}_1 \equiv Energy of the system at time t_1

\hat{E}_2 \equiv " " " " " " " " t_2

\dot{Q} \equiv Heat transfer from the surrounding to the system.

\dot{W} \equiv work done by the surrounding to the system.

$\dot{\eta}_1$ \equiv Energy associated with mass flow in

$\dot{\eta}_0$ \equiv " " " " " " " " out

\dot{m}_i \equiv mass flow rate entering the system.

\dot{m}_o \equiv " " " " " " " " leaving " " "

M_1 \equiv Mass of the system at time t_1

M_2 \equiv " " " " " " " " t_2

Energy balance: $M_2 \hat{E}_2 - M_1 \hat{E}_1 = [\dot{m}_i \dot{\eta}_i - \dot{m}_o \dot{\eta}_o + \dot{Q} - \dot{W}] \Delta t$

$\hat{E} = PE = \frac{gh}{g_c}$ $KE = \frac{1}{2} \frac{V^2}{g_c}$ $\hat{U} = f(T, P)$

$\hat{W}_p = PV$

$\hat{H} = \hat{U} + \hat{W}_p$

$$\dot{M}_2 [\hat{K}E_2 + \hat{P}E_2 + \hat{U}_2] - \dot{M}_1 [\hat{K}E_1 + \hat{P}E_1 + \hat{U}_1] =$$

$$\dot{m}_i [\hat{K}E_i + \hat{P}E_i + \hat{H}_i] - \dot{M}_o [\hat{K}E_o + \hat{P}E_o + \hat{H}_o] + \dot{Q} - \dot{W}$$

$$\Delta KE + \Delta PE + \Delta U = \dot{m}_i [\hat{K}E_i + \hat{P}E_i + \hat{H}_i] - \dot{M}_o [\hat{K}E_o + \hat{P}E_o + \hat{H}_o] + \dot{Q} - \dot{W}$$

closed system: $m_i = m_o = 0 \Rightarrow \Delta KE + \Delta PE + \Delta U = Q - W$

chemical process (closed system) $\rightarrow \Delta U = Q - W$

if no work $\boxed{\Delta U = Q}$

open system: ($m_i = m_o$)

$$\Delta H + \Delta PE + \Delta KE = Q - W \Rightarrow Q - W = \Delta H \Rightarrow \boxed{\Delta H = Q} \text{ chemical reaction}$$

Mechanical Energy Balance:

1. in compressible flow
2. single flow
3. liquid flow
4. No chemical reaction
5. steady state (open)

$$H = U + PV \rightarrow \hat{H} = u + \frac{P}{\rho} \Rightarrow \Delta \hat{H} = \Delta u + \frac{\Delta P}{\rho}$$

$$0 = \dot{m}_i [\hat{K}E_i + \hat{P}E_i + \hat{H}_i] - \dot{m}_o (\hat{K}E_o + \hat{P}E_o + \hat{H}_o) + \dot{Q} - \dot{W}$$

$$\Delta KE + \Delta PE + \Delta U + \frac{\Delta P}{\rho} = Q - W$$

Friction $\rightarrow F = \Delta U - Q$

$$\boxed{\frac{\Delta P}{\rho} + \Delta KE + \Delta PE + F = -W}$$

$$\frac{\Delta P}{\rho} + \Delta KE + \Delta PE + F = 0 \quad \text{No work}$$

$$\frac{\Delta P}{\rho} + \Delta KE + \Delta PE = 0 \quad \text{Bernulli Equation (No friction)}$$

Hw: ch 21: 31, 35, 38 | important pages: page 703
 ch 22: 7, 11, 17, 33 | enthalpy chart, stable E,
 ch 23: 16, 32, 49 | heat capacity, Appendix F-XD

$$u = f(T, V)$$

$$du = \left(\frac{du}{dT} \right)_V dT + \left(\frac{du}{dV} \right)_T dV \rightarrow c_v = \left(\frac{du}{dT} \right)_V$$

$$\Rightarrow du = c_v dT \Rightarrow \Delta u = \int_{T_{ref}}^T c_v dT$$

دما و حجم ثابت
مقدار

$$H = f(T, P) : dH = \left(\frac{dH}{dT} \right)_P dT + \left(\frac{dH}{dP} \right)_T dP$$

$$c_p = \left(\frac{dH}{dT} \right)_P \rightarrow \Delta H = \int c_p dT$$

$$c_p = a + bT + cT^2 + dT^3$$

$c_p \approx c_v$ for solid & liquid

$c_p = c_v + R$ for ideal gas

↑
gas constant

mixtures:

$$\text{open} \quad \Delta H_{total} = \sum_{i=1}^n n_i \Delta H_i$$

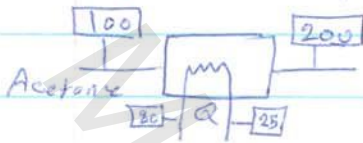
c_1	$x(1,1)$	$\hat{H}(1,1)$	$H(1,1)$	$Q = H_0 - H_1$ $\rightarrow Q = H_3 - (H_1 + H_2)$
c_2	$x(2,1)$	$\hat{H}(2,1)$	$H(2,1)$	
c_3	$x(3,1)$	$\hat{H}(3,1)$	$H(3,1)$	
			$\underline{H_1}$	

$$\Delta H_{total} = \sum_{i=1}^n n_i \Delta H_i = n_T \sum_{i=1}^n y_i \Delta H_i$$

↑
mole fraction

$$\Delta H_{total} = n_T \sum_{i=1}^n y_i \int_{T_1}^{T_2} c_{p_i} dT$$

example: چقدر آب لازم است تا استاستن را از 100 به 200 برساند



state	form	T	a	$b \times 10^2$	$c \times 10^5$	$d \times 10^9$	
g	1	$^{\circ}\text{C}$	71.96	20.1	-12.78	34.76	$0-1200$

$$c_p = 71.96 + 20.1 \times 10^{-2} T - 12.78 \times 10^{-5} T^2 + 34.76 \times 10^{-9} T^3$$

$$Q_1 = m_1 \int_{25}^{100} c_p dT$$

← استاستن

$$\text{Acetane } Q_2 = m_2 \int_{100}^{200} c_p dT$$

← Acetane

$$\rightarrow Q_1 = Q_2 \rightarrow m_1 =$$

از لحاظ Material بسته است ولی energy باز است. closed system:

$$\Delta PE + \Delta KE + \Delta U = Q - W \rightarrow \Delta U = Q - W$$

سیستم به ما کار داده +
ما به سیستم کار ردیم -
گرماگیر +
گرمادار -

No shaft work $\Delta U = Q$ اگر کار مکانیکی نداشته باشیم:

جدول نمودار رابطه ریاضی

$$Q = \int_{T_1}^{T_2} \rho c_v dT$$

روشنی های بدست آوردن U
گرمای ویژه در حجم ثابت

$$Q = u_2 - u_1$$

open system: مجموع انرژی درونی و کار انجام شده توسط سیال

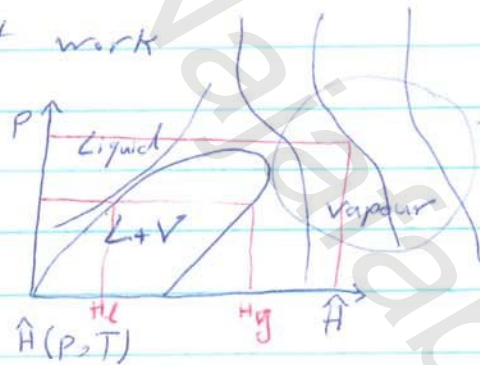
$$\Delta PE + \Delta KE + \Delta H = Q - W \rightarrow \Delta H = Q - W$$

به علت اختلاف ارتفاع
به انرژی پتانسیل وجود دارد
اختلاف دلی تاچیناس (نسبت به ΔH)

به علت اختلاف سرعت وجود دارد
دلی تاچیناس (نسبت به ΔH)

$\Delta H = Q$ No shaft work

ΔH جدول نمودار رابطه ریاضی



جدول آخر کتاب (برای تبدیل آب ۱۰۰ به بخار آب ده) $h_{fg} = \Delta H$ دمای پنهانی ویژه $V = \frac{m}{\rho}$

نکته: $\hat{H} = u + Pv$ حجم ویژه انرژی درونی ویژه

$$\begin{cases} \hat{H}_f = u_f + Pv_f \\ \hat{H}_g = u_g + Pv_g \end{cases}$$

$$Q = m \int_{T_1}^{T_2} c_p(T) dT = \Delta H \quad (\text{جدول E})$$

نکته: باید توجه کنیم که c_p با دما تغییر می‌کند

$$\hat{H}(T) = \int_{T_{ref}}^T c_p dT \quad (\text{جدول D})$$

مقدارهای \hat{H} در این جدول استوار نیست و می‌تواند بر اساس ΔH رابطه آوریم.

Mechanical Energy Balance:

$$\frac{\Delta P}{\rho} + \frac{\Delta V^2}{2g_c} + \frac{\Delta Z g}{g_c} + F = \frac{w}{m}$$

↓
Friction Factor

closed system:

Example 1: A vessel contains 100 kg of water at 40°C, 50 psi. How much heat is required, to heat the water to 90°C

(Note: for liquid & solid: $c_v \approx c_p$)

جواب:

$$Q = \Delta U \rightarrow Q = m \int_{T_1}^{T_2} c_v dT \approx m \int_{T_1}^{T_2} c_p dT$$

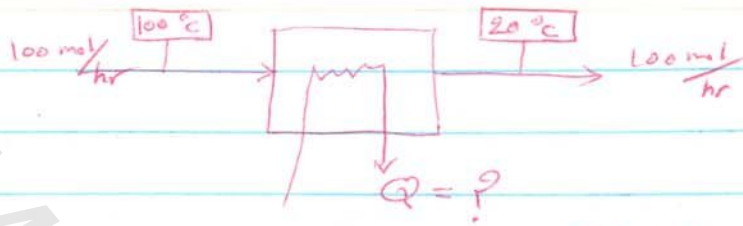
جواب:

$$Q = m (\hat{u}_2 - \hat{u}_1) = 100 \text{ kg} (376.9 - 167.4) \frac{\text{kJ}}{\text{kg}}$$

$$\rightarrow \boxed{Q = 20950 \text{ kJ}}$$

open system:

Examp 2: 100 mol/hr of N_2 gas entering a heat exchanger at 100°C and leaving at 20°C. calculate the amount of heat that must be removed?



$$Q = m \Delta H \quad \text{① روشی}$$

$$Q = m (\hat{H}(20^\circ\text{C}) - \hat{H}(100^\circ\text{C})) \quad \text{② روشی}$$

$$Q = m \int_{100}^{20} c_p dT \quad \text{③ روشی}$$

$c_p \left(\frac{\text{J}}{\text{mol} \cdot ^\circ\text{C}} \right)$

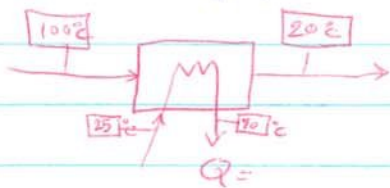
$$\text{④ روشی} \quad Q = 100 \frac{\text{mol}}{\text{hr}} \int_{100}^{20} (29 + 0.2197 \times 10^{-2} T + 0.5723 \times 10^{-5} T^2 - 2.876 \times 10^{-9} T^3) dT$$

$$\rightarrow Q = -23234 \frac{\text{J}}{\text{hr}}$$

Example 3:

از مثال قبلی برای گرم کردن آب استفاده : مثل قبلی

شود چه مقدار آب می توان گرم کرد (آب از 25 °C به 90 °C) ؟



$$Q = m \Delta H$$

$$Q = m (\hat{H}(90^\circ\text{C}) - \hat{H}(25^\circ\text{C})) = m (376.9 - 104.8) \frac{\text{kJ}}{\text{kg}} \times \frac{18 \text{ g}}{\text{mol}}$$

$$= 23234 \frac{\text{J}}{\text{hr}}$$

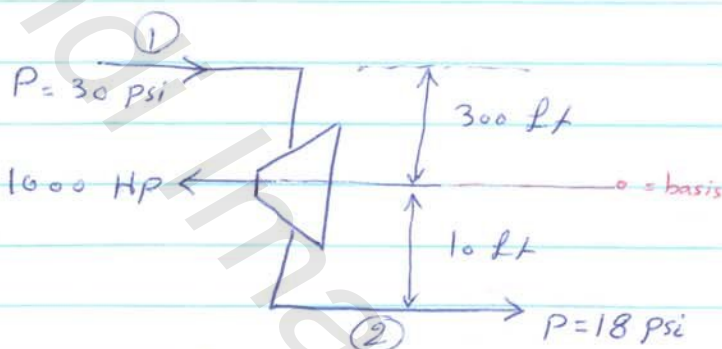
مقدار آب گرم

Mechanical Energy Balance:

Example 3: consider the following schematic for electric power. Determine the water flow through the turbine. Given the condition at the left. The conducts are of constant cross section and there are no losses.

$$\frac{\Delta V^2}{2g_c} = 0$$

$$F = 0$$



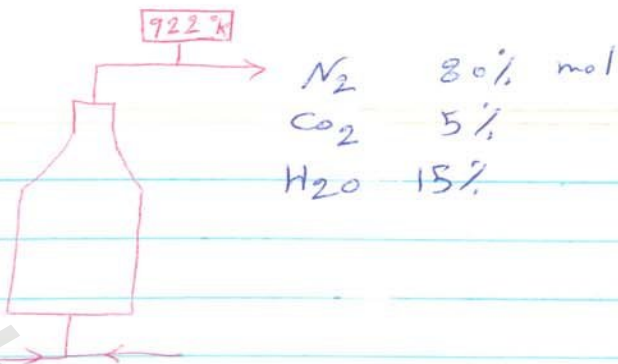
$$F + \frac{\Delta P}{\rho} + \frac{\Delta V^2}{2g_c} + \frac{g \Delta z}{g_c} = -\frac{W}{\dot{m}}$$

$$\frac{(18 - 30) \frac{\text{lb}_f}{\text{in}^2} \frac{144 \text{ in}^2}{\text{ft}^2}}{62.4 \frac{\text{lb}_m}{\text{ft}^3}} + \frac{(-10 - 300) \text{ ft} \cdot 32.2 \frac{\text{ft}}{\text{sec}^2}}{32.174 \frac{\text{lb}_m \cdot \text{ft}}{\text{lb}_f \cdot \text{sec}^2}} = \frac{-1000 \text{ HP} \cdot 550 \frac{\text{lb}_f \cdot \text{ft}}{\text{sec}}}{\dot{m} \left(\frac{\text{lb}_m}{\text{sec}} \right)}$$

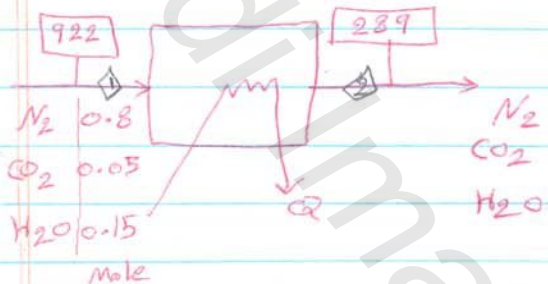
$$\rightarrow \dot{m} = 1627 \frac{\text{lb}_m}{\text{sec}}$$

Example 4: A stack gas leaves a furnace at 922°K and rapidly cools to the ambient temperature of 289°K . How much heat is given off to the surrounding if the composition of the gas is N_2 80% mol, CO_2 5% and H_2O 15%.

sol:



Basis: 1 Mole

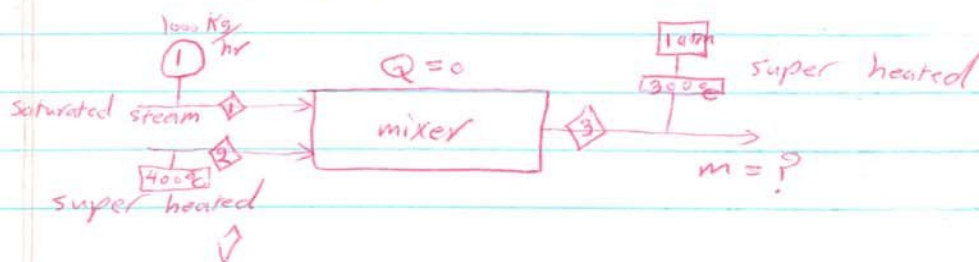


comp	X	\hat{H}	X	\hat{H}
N ₂	0.8	493	0.8	19667
CO ₂	0.05	616	0.05	29180
H ₂ O	0.15	588	0.15	22945
		H ₁		H ₂

$$Q = H_0 - H_1 = [X(1,2)\hat{H}(1,2) + X(2,2)\hat{H}(2,2) + X(3,2)\hat{H}(3,2)] - [X(1,1)\hat{H}(1,1) + X(2,1)\hat{H}(2,1) + X(3,1)\hat{H}(3,1)]$$

$$Q = 510.4 - 20634 = -20123.6 \text{ J}$$

Example 5: Saturated steam at 1 atm is discharged from a turbine at a rate of 1000 $\frac{\text{kg}}{\text{hr}}$. Super heated steam at 300°C and 1 atm is needed as a feed to a heat exchanger to produce it, the turbine discharged stream is mixed with super heated steam available from a second source at 400°C and 1 atm. The mixing unit operate adiabatically. Calculate the amount of steam at 300°C produced, and the required flow rate of the 400°C steam.



$out = in$
 material balance
 $\dot{m} = \dot{m}_1 + \dot{m}_2$

 $Q = \Delta H = 0$
 $\rightarrow H_0 = H_1$
 Energy balance

$$\dot{m}_3 \hat{H}(3) = \dot{m}_2 \hat{H}(2) + \dot{m}_1 \hat{H}(1)$$

$$\hat{H}(1) = 2676 \frac{\text{KJ}}{\text{kg}}$$

$$\hat{H}(2) = 32788$$

$$\hat{V} = 3.11 \frac{\text{m}^3}{\text{kg}}$$

$$\hat{H}(3) = 3074 \frac{\text{KJ}}{\text{kg}}$$

$$\rightarrow \dot{m}_3 (3074) = 1000 (2676) + \dot{m}_2 (32788)$$

$$\rightarrow \dot{m}_3 = 2951 \frac{\text{kg}}{\text{hr}}$$

$$\dot{m}_2 = 1951 \frac{\text{kg}}{\text{hr}}$$

$$\dot{V}_2 = \dot{m}_2 \hat{V}_2 = (1951 \frac{\text{kg}}{\text{hr}}) (3.11 \frac{\text{m}^3}{\text{kg}}) = 6067 \frac{\text{m}^3}{\text{hr}}$$

Chemical reaction: ($Q = \Delta H$)

$$Q = \Delta H \rightarrow \Delta H = \int_{T_{\text{ref}}}^T c_p dT \rightarrow \hat{H}(T) - \hat{H}(T_{\text{ref}}) = \int_{T_{\text{ref}}}^T c_p dT$$

$$\rightarrow \hat{H}(T) = \hat{H}(T_{\text{ref}}) + \int_{T_{\text{ref}}}^T c_p dT \rightarrow \hat{H}(T) = \Delta \hat{H}_f + \int_{T_{\text{ref}}}^T c_p dT$$



$$Q = \Delta H = (1) \hat{H}_{\text{CO}_2} - (1) \hat{H}_{\text{CO}} + \left(\frac{1}{2}\right) \hat{H}_{\text{O}_2}$$

$$Q = \left[\Delta \hat{H}_{f_{\text{CO}_2}} + \int_{25}^{25} c_{p_{\text{CO}_2}} dT \right] - \left[\Delta \hat{H}_{f_{\text{CO}}} + \int_{25}^{25} c_{p_{\text{CO}}} dT \right] -$$

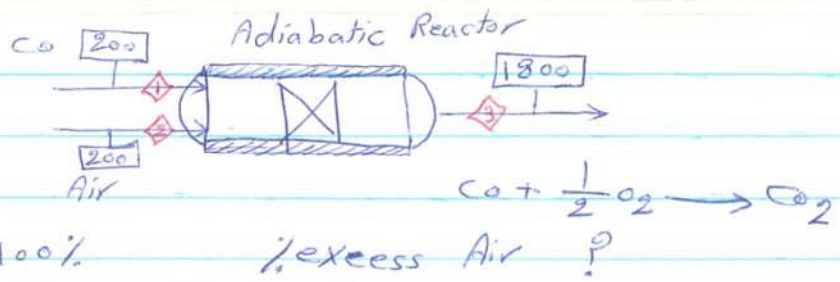
$$\left[\frac{1}{2} \left(\Delta \hat{H}_{f_{\text{O}_2}} + \int_{25}^{25} c_{p_{\text{O}_2}} dT \right) \right] \rightarrow$$

$$Q = \Delta \hat{H}_{f_{\text{CO}_2}} - \left(\Delta \hat{H}_{f_{\text{CO}}} + \frac{1}{2} \Delta \hat{H}_{f_{\text{O}_2}} \right)$$

$$\text{موسول: } \hat{H}(I, J) = \Delta \hat{H}_f(I, J) + \underbrace{\int_{T_{\text{ref}}}^T c_p(I, J) dT}_{H(I, J)}$$

$$Q = \Delta H_R + \Delta H$$

Example 6:



Comp	①	②	③	
CO	100%	0	0	6 unknown
CO ₂	0	0	X(2,3)	1 Basis
O ₂	0	21%	X(3,3)	3 MB
N ₂	0	79%	X(4,3)	1 Def
	S ₁	S ₂	S ₃	5 } → 6
				energy balance

1 unknown from energy balance: $Q = \Delta H = 0 \rightarrow H_0 = H_f$

$$* \rightarrow X(2,3) \hat{H}(2,3) + X(3,3) \hat{H}(3,3) + X(4,3) \hat{H}(4,3) = S_1 \hat{H}(1,1) + 0.21 S_2 \hat{H}(3,2) + 0.79 S_2 \hat{H}(4,3)$$

① $S_1 = 1$ mole

② $S_2 = S_1$ mole CO | $\frac{1}{2} O_2$ | X mole Feed | Air

1	S ₁	1	not Required	0.21 O ₂
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③ $X(2,3) = S_1$ CO | $\frac{1}{1} CO_2$

④ $X(3,3) = 0.21 S_2 = 1$ mole / S₁ CO | $\frac{1}{1} CO$ | $\frac{1}{2} O_2$

⑤ $X(4,3) = 0.79 S_2$

⑥ $S_3 = X(2,3) + X(3,3) + X(4,3)$

	$\Delta \hat{H}_f$ (Btu/gral)	$\frac{\int \bar{c}_p dT}{\Delta T}$	\bar{c}_{p_m} (200 °F)	\bar{c}_{p_m} (1800 °F)
CO ₂	-169,315		9.203	11.880
CO	-47,554		6.981	7.566
O ₂	0		7.114	7.946
N ₂	0		6.967	7.480

$$\hat{H}(I, J) = \Delta \hat{H}_f(I, J) + \int_{77^\circ F}^{T_J} \bar{c}_p(I, J) dT$$

$\hat{H}(I, J)$

$$\rightarrow \hat{H}(1, 1) = -46695 \frac{\text{Btu}}{\text{lbmol}}$$

$$\hat{H}(3, 2) = 879$$

$$\hat{H}(4, 2) = 857$$

$$\hat{H}(2, 3) = -148846$$

$$\hat{H}(3, 3) = 13690$$

$$\hat{H}(4, 3) = 12888$$

$$\rightarrow \text{(*) } X = 3.77$$

$$\rightarrow \% \text{ excess Air} = \frac{X-1}{1} \times 100 = 277\%$$

Ideal Gas :

$$PV = nRT$$

Real Gas :

$$PV = Z nRT$$



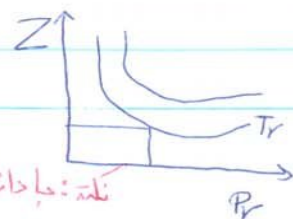
Deviation from ideal Gas

$$V_r = \frac{V}{V_c}$$

$$P_r = \frac{P}{P_c}$$

$$T_r = \frac{T}{T_c}$$

$$Z = \frac{V_{\text{actual}}}{V_{\text{ideal}}}$$



نکته: با داشتن $Z \leftarrow P_r, T_r$ می توانیم Z را پیدا کنیم.