

1-

$$(a) \quad t_{rr} \cong \sqrt{\frac{2Q_{RR}}{di/dt}}$$

$$Q_{RR} = 0.5 (di/dt) t_{rr}^2 = 0.5 \times 80 \times 5^2 \times 10^{-6} = 1000 \mu\text{C}$$

$$(b) \quad I_{RR} = \sqrt{2Q_{RR} \frac{di}{dt}}$$

$$I_{RR} = \sqrt{2Q_{RR} \frac{di}{dt}} = \sqrt{2 \times 1000 \times 80} = 400 \text{ A}$$

2-

$$= \frac{V_m}{\pi} (1 - \cos \omega t_{rr})$$

With zero reverse recovery time, average output voltage,

is

$$V_0 = \frac{2\sqrt{2} \times 230}{\pi} = 207.04 \text{ V}$$

(a) For  $f = 50 \text{ Hz}$  and  $t_{rr} = 40 \mu\text{s}$ , the reduction in the average output voltage,

is

$$\begin{aligned} V_r &= \frac{V_m}{\pi} (1 - \cos 2\pi f t_{rr}) \\ &= \frac{\sqrt{2} \times 230}{\pi} \left( 1 - \cos 2\pi \times 50 \times 40 \times 10^{-6} \times \frac{180}{\pi} \right) \\ &= 8.174 \text{ mV} \end{aligned}$$

Percentage reduction in average output voltage

$$= \frac{8.174 \times 10^{-3}}{207.04} \times 100 = 3.948 \times 10^{-3} \%$$

(b) For  $f = 2500 \text{ Hz}$ , the reduction in the average output voltage,

is

$$\begin{aligned} V_r &= \frac{\sqrt{2} \times 230}{\pi} \left( 1 - \cos 2\pi \times 2500 \times 40 \times 10^{-6} \times \frac{180}{\pi} \right) \\ &= 19.77 \text{ V} \end{aligned}$$

Percentage reduction in average output voltage =  $\frac{19.77}{207.04} \times 100 = 9.594\%$ .

It is seen from above that the effect of reverse recovery time is negligible for diode operation at 50 Hz, but for high-frequency operation of diodes, the effect is noticeable.

3-

$f = 250 \text{ Hz}$ . Use the average output voltage to calculate the load inductance  $L$ , which would limit the maximum load ripple current to 10% of  $I_a$ .

### Solution

$V_s = 550 \text{ V}$ ,  $R = 0.25 \Omega$ ,  $E = 0 \text{ V}$ ,  $f = 250 \text{ Hz}$ ,  $T = 1/f = 0.004 \text{ s}$ , and  $\Delta i = 200 \times 0.1 = 20 \text{ A}$ . The average output voltage  $V_a = kV_s = RI_a$ . The voltage across the inductor is given by

$$L \frac{di}{dt} = V_s - RI_a = V_s - kV_s = V_s(1 - k)$$

If the load current is assumed to rise linearly,  $dt = t_1 = kT$  and  $di = \Delta i$ :

$$\Delta i = \frac{V_s(1 - k)}{L} kT$$

For the worst-case ripple conditions,

$$\frac{d(\Delta i)}{dk} = 0$$

This gives  $k = 0.5$  and

$$\Delta i L = 20 \times L = 550(1 - 0.5) \times 0.5 \times 0.004$$

and the required value of inductance is  $L = 27.5$  mH.

4-

$V_s = 12$  V,  $\Delta V_c = 20$  mV,  $\Delta I = 0.8$  A,  $f = 25$  kHz, and  $V_a = 5$  V.

- a. From Eq. (5.48),  $V_a = kV_s$ , and  $k = V_a/V_s = 5/12 = 0.4167 = 41.67\%$ .
- b. From Eq. (5.51),

$$L = \frac{5(12 - 5)}{0.8 \times 25,000 \times 12} = 145.83 \mu\text{H}$$

- c. From Eq. (5.53),

$$C = \frac{0.8}{8 \times 20 \times 10^{-3} \times 25,000} = 200 \mu\text{F}$$

- d. From Eq. (5.56), we get  $L_c = \frac{(1 - k)R}{2f} = \frac{(1 - 0.4167) \times 500}{2 \times 25 \times 10^3} = 5.83$  mH

$$\text{From Eq. (5.57), we get } C_c = \frac{1 - k}{16Lf^2} = \frac{1 - 0.4167}{16 \times 5.83 \times 10^{-2} \times (25 \times 10^3)^2} = 0.4 \mu\text{F}$$

5-

- a. From Eq. (6.3),  $V_{o1} = 0.45 \times 48 = 21.6$  V.
- b. From Eq. (6.1),  $V_o = V_s/2 = 48/2 = 24$  V. The output power,  $P_o = V_o^2/R = 24^2/2.4 = 240$  W.
- c. The peak transistor current  $I_p = 24/2.4 = 10$  A. Because each transistor conducts for a 50% duty cycle, the average current of each transistor is  $I_Q = 0.5 \times 10 = 5$  A.
- d. The peak reverse blocking voltage  $V_{BR} = 2 \times 24 = 48$  V.
- e. From Eq. (6.3),  $V_{o1} = 0.45V_s$ , and the rms harmonic voltage  $V_h$

$$V_h = \left( \sum_{n=3,5,7,\dots}^{\infty} V_{on}^2 \right)^{1/2} = (V_o^2 - V_{o1}^2)^{1/2} = 0.2176V_s$$

From Eq. (6.8), THD =  $(0.2176V_s)/(0.45V_s) = 48.34\%$ .

- f. From Eq. (6.2), we can find  $V_{on}$  and then find,

$$\left[ \sum_{n=3,5,\dots}^{\infty} \left( \frac{V_{on}}{n^2} \right)^2 \right]^{1/2} = \left[ \left( \frac{V_{o3}}{3^2} \right)^2 + \left( \frac{V_{o5}}{5^2} \right)^2 + \left( \frac{V_{o7}}{7^2} \right)^2 + \dots \right]^{1/2} = 0.024V_s$$

From Eq. (6.9), DF =  $0.024V_s/(0.45V_s) = 5.382\%$ .

6-

$V_s = 220$  V,  $R = 5 \Omega$ ,  $L = 23$  mH,  $f_0 = 60$  Hz, and  $\omega = 2\pi \times 60 = 377$  rad/s.

- a. Using Eq. (6.16a), the instantaneous line-to-line voltage  $v_{ab}(t)$  can be written as

$$v_{ab}(t) = 242.58 \sin(377t + 30^\circ) - 48.52 \sin 5(377t + 30^\circ) \\ - 34.66 \sin 7(377t + 30^\circ) + 22.05 \sin 11(377t + 30^\circ) \\ + 18.66 \sin 13(377t + 30^\circ) - 14.27 \sin 17(377t + 30^\circ) + \dots$$

$$Z_L = \sqrt{R^2 + (n\omega L)^2} / \tan^{-1}(n\omega L/R) = \sqrt{5^2 + (8.67n)^2} / \tan^{-1}(8.67n/5)$$

Using Eq. (6.22), the instantaneous line (or phase) current is given by

$$i_a(t) = 14 \sin(377t - 60^\circ) - 0.64 \sin(5 \times 377t - 83.4^\circ) \\ - 0.33 \sin(7 \times 377t - 85.3^\circ) + 0.13 \sin(11 \times 377t - 87^\circ) \\ + 0.10 \sin(13 \times 377t - 87.5^\circ) - 0.06 \sin(17 \times 377t - 88^\circ) - \dots$$

- b. From Eq. (6.17),  $V_L = 0.8165 \times 220 = 179.63$  V.
- c. From Eq. (6.20),  $V_p = 0.4714 \times 220 = 103.7$  V.
- d. From Eq. (6.19),  $V_{L1} = 0.7797 \times 220 = 171.53$  V.
- e.  $V_{p1} = V_{L1}/\sqrt{3} = 99.03$  V.
- f. From Eq. (6.19),  $V_{L1} = 0.7797V_s$

$$\left( \sum_{n=5,7,11,\dots}^{\infty} V_{Ln}^2 \right)^{1/2} = (V_L^2 - V_{L1}^2)^{1/2} = 0.24236V_s$$

From Eq. (6.8), THD =  $0.24236V_s/(0.7797V_s) = 31.08\%$ . The rms harmonic line voltage is

$$g. V_{Lh} = \left[ \sum_{n=5,7,11,\dots}^{\infty} \left( \frac{V_{Ln}}{n^2} \right)^2 \right]^{1/2} = 0.00941V_s$$

From Eq. (6.9), DF =  $0.00941V_s/(0.7797V_s) = 1.211\%$ .